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NPTEL : Measure and Integration (Mathematics)

Co-ordinators : Prof. Inder K Rana

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Lecture 6 - The Length function and its properties

Lecture 7 - Countably additive set functions on intervals

Lecture 8 - Uniqueness Problem for Measure

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Lecture 11 - Measurable sets

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DIGIMAT - The No.1 Learning Management Platform for Creative Learning

NPTEL : Mathematics in India - From Vedic Period to Modern Times (Mathematics)

Co-ordinators : Prof. M.D. Srinivas, Prof. K. Ramasubramanian, Prof. M.S. Sriram

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- Lecture 1 - Basic Problem in Topology
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- Lecture 3 - Bird's eye-view of the course
- Lecture 4 - Path Homotopy
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- Lecture 6 - Fundamental group π_1
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- Lecture 9 - Computation concluded
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- Lecture 13 - Group Actions
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- Lecture 17 - Quotient Constructions (Continued...)
- Lecture 18 - Relative Homotopy
- Lecture 19 - Construction of a typical SDR
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- Lecture 24 - General Remarks
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- Lecture 26 - Abstract Simplicial Complex
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- Lecture 32 - Barycentric Subdivision
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- Lecture 55 - Classification of G-coverings
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- Lecture 57 - Pushouts and Free products
- Lecture 58 - Existence of Free Products, pushouts
- Lecture 59 - Free Products and free groups
- Lecture 60 - Seifert-Van Kampen Theorems
- Lecture 61 - Applications
- Lecture 62 - Applications (Continued...)

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Lecture 3 - Subcomplexes and Examples

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Lecture 5 - More Examples

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Lecture 9 - Product of Cell complexes

Lecture 10 - Product of Cell complexes (Continued...)

Lecture 11 - Partition of Unity on CW-complexes

Lecture 12 - Partition of Unity (Continued...)

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Lecture 14 - Homotopical Aspects (Continued...)

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Lecture 16 - Cellular Maps (Continued...)

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- Lecture 32 - Applications
- Lecture 33 - Applications (Continued...)
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- Lecture 39 - CW structure and CW homology of Lens Spaces
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- Lecture 50 - Manifolds with Boundary
- Lecture 51 - Embeddings and Homotopical Aspects
- Lecture 52 - Homotopical Aspects (Continued...)
- Lecture 53 - Classification of 1-manifolds
- Lecture 54 - Classification of 1-manifolds (Continued...)
- Lecture 55 - Triangulation of Manifolds
- Lecture 56 - Pseudo-Manifolds
- Lecture 57 - One result due to Poincaré and another due to Munkres
- Lecture 58 - Some General Remarks
- Lecture 59 - Classification of Compact Surface
- Lecture 60 - Final Reduction-Completion of the Proof
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- Lecture 62 - Orientability

- Lecture 1 - Partial Differential Equations - Basic concepts and Nomenclature
- Lecture 2 - First Order Partial Differential Equations- How they arise? Cauchy Problems, IVPs, IBVPs
- Lecture 3 - First order Partial Differential Equations - Geometry of Quasilinear equations
- Lecture 4 - FOPDE's - General Solutions to Linear and Semilinear equations
- Lecture 5 - First order Partial Differential Equations- Lagrange's method for Quasilinear equations
- Lecture 6 - Relation between Characteristic curves and Integral surfaces for Quasilinear equations
- Lecture 7 - Relation between Characteristic curves and Integral surfaces for Quasilinear equations
- Lecture 8 - FOPDE's - Method of characteristics for Quasilinear equations - 1
- Lecture 9 - First order Partial Differential Equations - Failure of transversality condition
- Lecture 10 - First order Partial Differential Equations - Tutorial of Quasilinear equations
- Lecture 11 - FOPDE's - General nonlinear equations 1 - Search for a characteristic direction
- Lecture 12 - FOPDE's - General nonlinear equations 2 - Characteristic direction and characteristic strip
- Lecture 13 - FOPDE's - General nonlinear equations 3 - Finding an initial strip
- Lecture 14 - FOPDE's - General nonlinear equations 4 - Local existence and uniqueness theorem
- Lecture 15 - First order Partial Differential Equations - Tutorial on General nonlinear equations
- Lecture 16 - First order Partial Differential Equations - Initial value problems for Burgers equation
- Lecture 17 - FOPDE's - Conservation laws with a view towards global solutions to Burgers equation
- Lecture 18 - Second Order Partial Differential Equations - Special Curves associated to a PDE
- Lecture 19 - Second Order Partial Differential Equations - Curves of discontinuity
- Lecture 20 - Second Order Partial Differential Equations - Classification
- Lecture 21 - SOPDE's - Canonical form for an equation of Hyperbolic type
- Lecture 22 - SOPDE's - Canonical form for an equation of Parabolic type
- Lecture 23 - SOPDE's - Canonical form for an equation of Elliptic type
- Lecture 24 - Second Order Partial Differential Equations - Characteristic Surfaces
- Lecture 25 - SOPDE's - Canonical forms for constant coefficient PDEs
- Lecture 26 - Wave Equation - A mathematical model for vibrating strings
- Lecture 27 - Wave Equation in one space dimension - d'Alembert formula
- Lecture 28 - Tutorial on One dimensional wave equation
- Lecture 29 - Wave Equation in d space dimensions - Equivalent Cauchy problems via Spherical means
- Lecture 30 - Cauchy problem for Wave Equation in 3 space dimensions - Poisson-Kirchhoff formulae
- Lecture 31 - Cauchy problem for Wave Equation in 2 space dimensions - Hadamard's method of descent

- Lecture 32 - Nonhomogeneous Wave Equation - Duhamel principle
- Lecture 33 - Wellposedness of Cauchy problem for Wave Equation
- Lecture 34 - Wave Equation on an interval in? - Solution to an IBVP from first principles
- Lecture 35 - Tutorial on IBVPs for wave equation
- Lecture 36 - IBVP for Wave Equation - Separation of Variables Method
- Lecture 37 - Tutorial on Separation of variables method for wave equation
- Lecture 38 - Qualitative analysis of Wave equation - Parallelogram identity
- Lecture 39 - Qualitative analysis of Wave equation - Domain of dependence, domain of influence
- Lecture 40 - Qualitative analysis of Wave equation - Causality Principle, Finite speed of propagation
- Lecture 41 - Qualitative analysis of Wave equation - Uniqueness by Energy method
- Lecture 42 - Qualitative analysis of Wave equation - Huygens Principle
- Lecture 43 - Qualitative analysis of Wave equation - Generalized solutions to Wave equation
- Lecture 44 - Qualitative analysis of Wave equation - Propagation of waves
- Lecture 45 - Laplace equation - Associated Boundary value problems
- Lecture 46 - Laplace equation - Fundamental solution
- Lecture 47 - Dirichlet BVP for Laplace equation - Green's function and Poisson's formula
- Lecture 48 - Laplace equation - Weak maximum principle and its applications
- Lecture 49 - Laplace equation - Dirichlet BVP on a disk in \mathbb{R}^2 for Laplace equations
- Lecture 50 - Tutorial 1 on Laplace equation
- Lecture 51 - Laplace equation - Mean value property
- Lecture 52 - Laplace equation - More qualitative properties
- Lecture 53 - Laplace equation - Strong Maximum Principle and Dirichlet Principle
- Lecture 54 - Tutorial 2 on Laplace equation
- Lecture 55 - Cauchy Problem for Heat Equation - 1
- Lecture 56 - Cauchy Problem for Heat Equation - 2
- Lecture 57 - IBVP for Heat equation Subtitle: Method of Separation of Variables
- Lecture 58 - Maximum principle for heat equation
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NPTEL : NOC:Point Set Topology (Mathematics)

Co-ordinators : Prof. Ronnie Sebastian

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Lecture 22 - Connectedness of $GL(n, \mathbb{C})$, $SL(n, \mathbb{C})$, $SL(n, \mathbb{R})$

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Lecture 28 - Compact metric spaces

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NPTEL : Stochastic Processes (Mathematics)

Co-ordinators : Dr. S. Dharmaraja

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Lecture 2 - Introduction to Stochastic Processes (Continued.)

Lecture 3 - Problems in Random Variables and Distributions

Lecture 4 - Problems in Sequences of Random Variables

Lecture 5 - Definition, Classification and Examples

Lecture 6 - Simple Stochastic Processes

Lecture 7 - Stationary Processes

Lecture 8 - Autoregressive Processes

Lecture 9 - Introduction, Definition and Transition Probability Matrix

Lecture 10 - Chapman-Kolmogorov Equations

Lecture 11 - Classification of States and Limiting Distributions

Lecture 12 - Limiting and Stationary Distributions

Lecture 13 - Limiting Distributions, Ergodicity and Stationary Distributions

Lecture 14 - Time Reversible Markov Chain, Application of Irreducible Markov Chain in Queueing Models

Lecture 15 - Reducible Markov Chains

Lecture 16 - Definition, Kolmogorov Differential Equations and Infinitesimal Generator Matrix

Lecture 17 - Limiting and Stationary Distributions, Birth Death Processes

Lecture 18 - Poisson Processes

Lecture 19 - M/M/1 Queueing Model

Lecture 20 - Simple Markovian Queueing Models

Lecture 21 - Queueing Networks

Lecture 22 - Communication Systems

Lecture 23 - Stochastic Petri Nets

Lecture 24 - Conditional Expectation and Filtration

Lecture 25 - Definition and Simple Examples

Lecture 26 - Definition and Properties

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Lecture 28 - Stochastic Differential Equations

Lecture 29 - Ito Integrals

Lecture 30 - Ito Formula and its Variants

Lecture 31 - Some Important SDE's and Their Solutions

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[Lecture 34 - Markov Renewal and Markov Regenerative Processes](#)

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Lecture 2 - Probability space and conditional probability

Lecture 3 - Random variable and cumulative distributive function

Lecture 4 - Discrete Uniform Distribution, Binomial Distribution, Geometric Distribution, Continuous Uniform Distribution, Exponential Distribution, Normal Distribution and Poisson Distribution

Lecture 5 - Joint Distribution of Random Variables

Lecture 6 - Independent Random Variables, Covariance and Correlation Coefficient and Conditional Distribution

Lecture 7 - Conditional Expectation and Covariance Matrix

Lecture 8 - Generating Functions, Law of Large Numbers and Central Limit Theorem

Lecture 9 - Problems in Random variables and Distributions

Lecture 10 - Problems in Random variables and Distributions (Continued...)

Lecture 11 - Problems in Random variables and Distributions (Continued...)

Lecture 12 - Problems in Random variables and Distributions (Continued...)

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Lecture 15 - Problems in Sequences of Random Variables (Continued...)

Lecture 16 - Problems in Sequences of Random Variables (Continued...)

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Lecture 18 - Classification of Stochastic Processes

Lecture 19 - Examples of Classification of Stochastic Processes

Lecture 20 - Examples of Classification of Stochastic Processes (Continued...)

Lecture 21 - Bernoulli Process

Lecture 22 - Poisson Process

Lecture 23 - Poisson Process (Continued...)

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Lecture 26 - Introduction to Discrete time Markov Chain (Continued...)

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NPTEL : Calculus of Variations and Integral Equations (Mathematics)

Co-ordinators : Dr. Malay Banerjee, Prof. D. Bahuguna

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NPTEL : Linear programming and Extensions (Mathematics)

Co-ordinators : Prof. Prabha Sharma

Lecture 1 - Introduction to Linear Programming Problems

Lecture 2 - Vector space, Linear independence and dependence, basis

Lecture 3 - Moving from one basic feasible solution to another, optimality criteria

Lecture 4 - Basic feasible solutions, existence & derivation

Lecture 5 - Convex sets, dimension of a polyhedron, Faces, Example of a polytope

Lecture 6 - Direction of a polyhedron, correspondence between bfs and extreme points

Lecture 7 - Representation theorem, LPP solution is a bfs, Assignment 1

Lecture 8 - Development of the Simplex Algorithm, Unboundedness, Simplex Tableau

Lecture 9 - Simplex Tableau & algorithm ,Cycling, Bland's anti-cycling rules, Phase I & Phase II

Lecture 10 - Big-M method,Graphical solutions, adjacent extreme pts and adjacent bfs

Lecture 11 - Assignment 2, progress of Simplex algorithm on a polytope, bounded variable LPP

Lecture 12 - LPP Bounded variable, Revised Simplex algorithm, Duality theory, weak duality theorem

Lecture 13 - Weak duality theorem, economic interpretation of dual variables, Fundamental theorem of duality

Lecture 14 - Examples of writing the dual, complementary slackness theorem

Lecture 15 - Complementary slackness conditions, Dual Simplex algorithm, Assignment 3

Lecture 16 - Primal-dual algorithm

Lecture 17 - Problem in lecture 16, starting dual feasible solution, Shortest Path Problem

Lecture 18 - Shortest Path Problem, Primal-dual method, example

Lecture 19 - Shortest Path Problem-complexity, interpretation of dual variables, post-optimality analysis-changes in the cost vector

Lecture 20 - Assignment 4, postoptimality analysis, changes in b, adding a new constraint, changes in $\{a_{ij}\}$, Parametric analysis

Lecture 21 - Parametric LPP-Right hand side vector

Lecture 22 - Parametric cost vector LPP

Lecture 23 - Parametric cost vector LPP, Introduction to Min-cost flow problem

Lecture 24 - Mini-cost flow problem-Transportation problem

Lecture 25 - Transportation problem degeneracy, cycling

Lecture 26 - Sensitivity analysis

Lecture 27 - Sensitivity analysis

Lecture 28 - Bounded variable transportation problem, min-cost flow problem

Lecture 29 - Min-cost flow problem

Lecture 30 - Starting feasible solution, Lexicographic method for preventing cycling ,strongly feasible solution

Lecture 31 - Assignment 6, Shortest path problem, Shortest Path between any two nodes,Detection of negative cycles

[Lecture 32 - Min-cost-flow Sensitivity analysis Shortest path problem sensitivity analysis](#)

[Lecture 33 - Min-cost flow changes in arc capacities , Max-flow problem, assignment 7](#)

[Lecture 34 - Problem 3 \(assignment 7\), Min-cut Max-flow theorem, Labelling algorithm](#)

[Lecture 35 - Max-flow - Critical capacity of an arc, starting solution for min-cost flow problem](#)

[Lecture 36 - Improved Max-flow algorithm](#)

[Lecture 37 - Critical Path Method \(CPM\)](#)

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NPTEL : Convex Optimization (Mathematics)

Co-ordinators : Dr. Joydeep Dutta

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NPTEL : Foundations of Optimization (Mathematics)

Co-ordinators : Dr. Joydeep Dutta

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Lecture 1 - Basic principles of counting

Lecture 2 - Sample space, events, axioms of probability

Lecture 3 - Conditional probability, Independence of events

Lecture 4 - Random variables, cumulative density function, expected value

Lecture 5 - Discrete random variables and their distributions

Lecture 6 - Discrete random variables and their distributions

Lecture 7 - Discrete random variables and their distributions

Lecture 8 - Continuous random variables and their distributions

Lecture 9 - Continuous random variables and their distributions

Lecture 10 - Continuous random variables and their distributions

Lecture 11 - Function of random variables, Moment generating function

Lecture 12 - Jointly distributed random variables, Independent r. v. and their sums

Lecture 13 - Independent r. v. and their sums

Lecture 14 - Chi χ^2 square r. v., sums of independent normal r. v., Conditional distr

Lecture 15 - Conditional distri, Joint distr. of functions of r. v., Order statistics

Lecture 16 - Order statistics, Covariance and correlation

Lecture 17 - Covariance, Correlation, Cauchy- Schwarz inequalities, Conditional expectation

Lecture 18 - Conditional expectation, Best linear predictor

Lecture 19 - Inequalities and bounds

Lecture 20 - Convergence and limit theorems

Lecture 21 - Central limit theorem

Lecture 22 - Applications of central limit theorem

Lecture 23 - Strong law of large numbers, Joint mgf

Lecture 24 - Convolutions

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Lecture 26 - Transition and state probabilities

Lecture 27 - State prob., First passage and First return prob

Lecture 28 - First passage and First return prob. Classification of states

Lecture 29 - Random walk, periodic and null states

Lecture 30 - Reducible Markov chains

Lecture 31 - Time reversible Markov chains

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Lecture 2 - Interesting Problems In Probability

Lecture 3 - Random variables, distribution function and independence

Lecture 4 - Chebyshev inequality, Borel-Cantelli Lemmas and related issues

Lecture 5 - Law of Large Number and Central Limit Theorem

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Lecture 7 - Conditional Expectation - II

Lecture 8 - Martingales

Lecture 9 - Brownian Motion - I

Lecture 10 - Brownian Motion - II

Lecture 11 - Brownian Motion - III

Lecture 12 - Ito Integral - I

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Lecture 14 - Ito Calculus - I

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Lecture 16 - Ito Integral In Higher Dimension

Lecture 17 - Application to Ito Integral - I

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- Lecture 2 - Countinuity And Compactness
- Lecture 3 - Countinuity And Connectdness
- Lecture 4 - Derivatives: Possible Definition
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- Lecture 15 - Specialisation to functions of two variables
- Lecture 16 - Implicit Function Theorem
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- Lecture 18 - Application of IFT: Lagrange's Multipliers Method
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- Lecture 20 - Application of IFT: Lagrange's Multipliers Method - c
- Lecture 21 - Application of IFT: Inverse Function Theorem - c

- Lecture 1 - Level curves and locus, definition of parametric curves, tangent, arc length, arc length parametrisation
- Lecture 2 - How much a curve is 'curved', signed unit normal and signed curvature, rigid motions, constant curvature
- Lecture 3 - Curves in \mathbb{R}^3 , principal normal and binormal, torsion
- Lecture 4 - Frenet-Serret formula
- Lecture 5 - Simple closed curve and isoperimetric inequality
- Lecture 6 - Surfaces and parametric surfaces, examples, regular surface and non-example of regular surface, transition maps.
- Lecture 7 - Transition maps of smooth surfaces, smooth function between surfaces, diffeomorphism
- Lecture 8 - Reparameterization
- Lecture 9 - Tangent, Normal
- Lecture 10 - Orientable surfaces
- Lecture 11 - Examples of Surfaces
- Lecture 12 - First Fundamental Form
- Lecture 13 - Conformal Mapping
- Lecture 14 - Curvature of Surfaces
- Lecture 15 - Euler's Theorem
- Lecture 16 - Regular Surfaces locally as Quadratic Surfaces
- Lecture 17 - Geodesics
- Lecture 18 - Existence of Geodesics, Geodesics on Surfaces of revolution
- Lecture 19 - Geodesics on surfaces of revolution; Clairaut's Theorem
- Lecture 20 - Pseudosphere
- Lecture 21 - Classification of Quadratic Surface
- Lecture 22 - Surface Area and Equiareal Map

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Lecture 6 - Estimation Of Parameters In Simple Linear Regression Model (Continued...)

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Lecture 12 - Estimation of Model Parameters in Multiple Linear Regression Model

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Lecture 15 - Testing of Hypothesis (Continued...) and Goodness of Fit of the Model

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Lecture 17 - Diagnostics in Multiple Linear Regression Model (Continued...)

Lecture 18 - Diagnostics in Multiple Linear Regression Model (Continued...)

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Lecture 23 - Outside Sample Forecasting

Lecture 24 - Software Implementation of Forecasting using MINITAB

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Lecture 2 - Why R and Installation Procedure

Lecture 3 - Introduction _Help_ Demo examples_ packages_ libraries

Lecture 4 - Introduction _Command line_ Data editor _ Rstudio

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Lecture 6 - Basics of Calculations _ Calculator _Built in Functions Assignments

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Lecture 9 - Basics Calculations: Matrix operations

Lecture 10 - Basics Calculations: Missing data and logical operators

Lecture 11 - Basics Calculations: Logical operators

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Lecture 13 - Basics Calculations: Conditional executions and loops

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Lecture 26 - Strings - Display and Formatting, Print and Format with Concatenate

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Lecture 30 - Strings - Display and Formatting, Replacement and Evaluation of Strings

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Lecture 11 - Subdivided Bar Plots and Pie Diagrams

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- Lecture 10 - LU Decomposition - Simplest Form
- Lecture 11 - Elementary Matrices
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- Lecture 13 - Row Reduced Echelon Form (RREF) (Continued...)
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- Lecture 32 - Rank-Nullity Theorem and Applications
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Lecture 14 - Line Integral in the Complex

Lecture 15 - Cauchy Integral Theorem

Lecture 16 - Cauchy Integral Theorem (Continued.)

Lecture 17 - Cauchy Integral Formula

Lecture 18 - Power and Taylor's Series of Complex Numbers

Lecture 19 - Power and Taylor's Series of Complex Numbers (Continued.)

Lecture 20 - Taylor's, Laurent Series of $f(z)$ and Singularities

Lecture 21 - Classification of Singularities, Residue and Residue Theorem

Lecture 22 - Laplace Transform and its Existence

Lecture 23 - Properties of Laplace Transform

Lecture 24 - Evaluation of Laplace and Inverse Laplace Transform

Lecture 25 - Applications of Laplace Transform to Integral Equations and ODEs

Lecture 26 - Applications of Laplace Transform to PDEs

Lecture 27 - Fourier Series

Lecture 28 - Fourier Series (Continued.)

Lecture 29 - Fourier Integral Representation of a Function

Lecture 30 - Introduction to Fourier Transform

Lecture 31 - Applications of Fourier Transform to PDEs

[Lecture 32 - Laws of Probability - I](#)

[Lecture 33 - Laws of Probability - II](#)

[Lecture 34 - Problems in Probability](#)

[Lecture 35 - Random Variables](#)

[Lecture 36 - Special Discrete Distributions](#)

[Lecture 37 - Special Continuous Distributions](#)

[Lecture 38 - Joint Distributions and Sampling Distributions](#)

[Lecture 39 - Point Estimation](#)

[Lecture 40 - Interval Estimation](#)

[Lecture 41 - Basic Concepts of Testing of Hypothesis](#)

[Lecture 42 - Tests for Normal Populations](#)

NPTEL : Functional Analysis (Mathematics)

Co-ordinators : Prof. P.D. Srivastava

- Lecture 1 - Metric Spaces with Examples
- Lecture 2 - Holder Inequality and Minkowski Inequality
- Lecture 3 - Various Concepts in a Metric Space
- Lecture 4 - Separable Metrics Spaces with Examples
- Lecture 5 - Convergence, Cauchy Sequence, Completeness
- Lecture 6 - Examples of Complete and Incomplete Metric Spaces
- Lecture 7 - Completion of Metric Spaces + Tutorial
- Lecture 8 - Vector Spaces with Examples
- Lecture 9 - Normed Spaces with Examples
- Lecture 10 - Banach Spaces and Schauder Basis
- Lecture 11 - Finite Dimensional Normed Spaces and Subspaces
- Lecture 12 - Compactness of Metric/Normed Spaces
- Lecture 13 - Linear Operators-definition and Examples
- Lecture 14 - Bounded Linear Operators in a Normed Space
- Lecture 15 - Bounded Linear Functionals in a Normed Space
- Lecture 16 - Concept of Algebraic Dual and Reflexive Space
- Lecture 17 - Dual Basis & Algebraic Reflexive Space
- Lecture 18 - Dual Spaces with Examples
- Lecture 19 - Tutorial - I
- Lecture 20 - Tutorial - II
- Lecture 21 - Inner Product & Hilbert Space
- Lecture 22 - Further Properties of Inner Product Spaces
- Lecture 23 - Projection Theorem, Orthonormal Sets and Sequences
- Lecture 24 - Representation of Functionals on a Hilbert Spaces
- Lecture 25 - Hilbert Adjoint Operator
- Lecture 26 - Self Adjoint, Unitary & Normal Operators
- Lecture 27 - Tutorial - III
- Lecture 28 - Annihilator in an IPS
- Lecture 29 - Total Orthonormal Sets And Sequences
- Lecture 30 - Partially Ordered Set and Zorns Lemma
- Lecture 31 - Hahn Banach Theorem for Real Vector Spaces

[Lecture 32 - Hahn Banach Theorem for Complex V.S. & Normed Spaces](#)

[Lecture 33 - Baires Category & Uniform Boundedness Theorems](#)

[Lecture 34 - Open Mapping Theorem](#)

[Lecture 35 - Closed Graph Theorem](#)

[Lecture 36 - Adjoint Operator](#)

[Lecture 37 - Strong and Weak Convergence](#)

[Lecture 38 - Convergence of Sequence of Operators and Functionals](#)

[Lecture 39 - LP - Space](#)

[Lecture 40 - LP - Space \(Continued.\)](#)

- Lecture 1 - Motivation with few Examples
- Lecture 2 - Single - Step Methods for IVPs
- Lecture 3 - Analysis of Single Step Methods
- Lecture 4 - Runge - Kutta Methods for IVPs
- Lecture 5 - Higher Order Methods/Equations
- Lecture 6 - Error - Stability - Convergence of Single Step Methods
- Lecture 7 - Tutorial - I
- Lecture 8 - Tutorial - II
- Lecture 9 - Multi-Step Methods (Explicit)
- Lecture 10 - Multi-Step Methods (Implicit)
- Lecture 11 - Convergence and Stability of multi step methods
- Lecture 12 - General methods for absolute stability
- Lecture 13 - Stability Analysis of Multi Step Methods
- Lecture 14 - Predictor - Corrector Methods
- Lecture 15 - Some Comments on Multi - Step Methods
- Lecture 16 - Finite Difference Methods - Linear BVPs
- Lecture 17 - Linear/Non - Linear Second Order BVPs
- Lecture 18 - BVPS - Derivative Boundary Conditions
- Lecture 19 - Higher Order BVPs
- Lecture 20 - Shooting Method BVPs
- Lecture 21 - Tutorial - III
- Lecture 22 - Introduction to First Order PDE
- Lecture 23 - Introduction to Second Order PDE
- Lecture 24 - Finite Difference Approximations to Parabolic PDEs
- Lecture 25 - Implicit Methods for Parabolic PDEs
- Lecture 26 - Consistency, Stability and Convergence
- Lecture 27 - Other Numerical Methods for Parabolic PDEs
- Lecture 28 - Tutorial - IV
- Lecture 29 - Matrix Stability Analysis of Finite Difference Scheme
- Lecture 30 - Fourier Series Stability Analysis of Finite Difference Scheme
- Lecture 31 - Finite Difference Approximations to Elliptic PDEs - I

- [Lecture 32 - Finite Difference Approximations to Elliptic PDEs - II](#)
- [Lecture 33 - Finite Difference Approximations to Elliptic PDEs - III](#)
- [Lecture 34 - Finite Difference Approximations to Elliptic PDEs - IV](#)
- [Lecture 35 - Finite Difference Approximations to Hyperbolic PDEs - I](#)
- [Lecture 36 - Finite Difference Approximations to Hyperbolic PDEs - II](#)
- [Lecture 37 - Method of characteristics for Hyperbolic PDEs - I](#)
- [Lecture 38 - Method of characterisitcs for Hyperbolic PDEs - II](#)
- [Lecture 39 - Finite Difference Approximations to 1st order Hyperbolic PDEs](#)
- [Lecture 40 - Summary, Appendices, Remarks](#)

NPTEL : Optimization (Mathematics)

Co-ordinators : Prof. A. Goswami, Dr. Debjani Chakraborty

Lecture 1 - Optimization - Introduction

Lecture 2 - Formulation of LPP

Lecture 3 - Geometry of LPP and Graphical Solution of LPP

Lecture 4 - Solution of LPP : Simplex Method

Lecture 5 - Big - M Method

Lecture 6 - Two - Phase Method

Lecture 7 - Special Cases in Simple Applications

Lecture 8 - Introduction to Duality Theory

Lecture 9 - Dual Simplex Method

Lecture 10 - Post Optimality Analysis

Lecture 11 - Integer Programming - I

Lecture 12 - Integer Programming - II

Lecture 13 - Introduction to Transportation Problems

Lecture 14 - Solving Various types of Transportation Problems

Lecture 15 - Assignment Problems

Lecture 16 - Project Management

Lecture 17 - Critical Path Analysis

Lecture 18 - PERT

Lecture 19 - Shortest Path Algorithm

Lecture 20 - Travelling Salesman Problem

Lecture 21 - Classical optimization techniques : Single variable optimization

Lecture 22 - Unconstrained multivariable optimization

Lecture 23 - Nonlinear programming with equality constraint

Lecture 24 - Nonlinear programming KKT conditions

Lecture 25 - Numerical optimization : Region elimination techniques

Lecture 26 - Numerical optimization : Region elimination techniques (Continued.)

Lecture 27 - Fibonacci Method

Lecture 28 - Golden Section Methods

Lecture 29 - Interpolation Methods

Lecture 30 - Unconstrained optimization techniques : Direct search method

Lecture 31 - Unconstrained optimization techniques : Indirect search method

[Lecture 32 - Nonlinear programming : constrained optimization techniques](#)

[Lecture 33 - Interior and Exterior penalty Function Method](#)

[Lecture 34 - Separable Programming Problem](#)

[Lecture 35 - Introduction to Geometric Programming](#)

[Lecture 36 - Constrained Geometric Programming Problem](#)

[Lecture 37 - Dynamic Programming Problem](#)

[Lecture 38 - Dynamic Programming Problem \(Continued.\)](#)

[Lecture 39 - Multi Objective Decision Making](#)

[Lecture 40 - Multi attribute decision making](#)

NPTEL : Probability and Statistics (Mathematics)

Co-ordinators : Prof. Somesh Kumar

Lecture 1 - Algebra of Sets - I

Lecture 2 - Algebra of Sets - II

Lecture 3 - Introduction to Probability

Lecture 4 - Laws of Probability - I

Lecture 5 - Laws of Probability - II

Lecture 6 - Problems in Probability

Lecture 7 - Random Variables

Lecture 8 - Probability Distributions

Lecture 9 - Characteristics of Distribution

Lecture 10 - Special Distributions - I

Lecture 11 - Special Distributions - II

Lecture 12 - Special Distributions - III

Lecture 13 - Special Distributions - IV

Lecture 14 - Special Distributions - V

Lecture 15 - Special Distributions - VI

Lecture 16 - Special Distributions - VII

Lecture 17 - Functions of a Random Variable

Lecture 18 - Joint Distributions - I

Lecture 19 - Joint Distributions - II

Lecture 20 - Joint Distributions - III

Lecture 21 - Joint Distributions - IV

Lecture 22 - Transformations of Random Vectors

Lecture 23 - Sampling Distributions - I

Lecture 24 - Sampling Distributions - II

Lecture 25 - Descriptive Statistics - I

Lecture 26 - Descriptive Statistics - II

Lecture 27 - Estimation - I

Lecture 28 - Estimation - II

Lecture 29 - Estimation - III

Lecture 30 - Estimation - IV

Lecture 31 - Estimation - V

[Lecture 32 - Estimation - VI](#)

[Lecture 33 - Testing of Hypothesis - I](#)

[Lecture 34 - Testing of Hypothesis - II](#)

[Lecture 35 - Testing of Hypothesis - III](#)

[Lecture 36 - Testing of Hypothesis - IV](#)

[Lecture 37 - Testing of Hypothesis - V](#)

[Lecture 38 - Testing of Hypothesis - VI](#)

[Lecture 39 - Testing of Hypothesis - VII](#)

[Lecture 40 - Testing of Hypothesis - VIII](#)

NPTEL : Regression Analysis (Mathematics)

Co-ordinators : Dr. Soumen Maity

Lecture 1 - Simple Linear Regression

Lecture 2 - Simple Linear Regression (Continued...1)

Lecture 3 - Simple Linear Regression (Continued...2)

Lecture 4 - Simple Linear Regression (Continued...3)

Lecture 5 - Simple Linear Regression (Continued...4)

Lecture 6 - Multiple Linear Regression

Lecture 7 - Multiple Linear Regression (Continued...1)

Lecture 8 - Multiple Linear Regression (Continued...2)

Lecture 9 - Multiple Linear Regression (Continued...3)

Lecture 10 - Selecting the BEST Regression model

Lecture 11 - Selecting the BEST Regression model (Continued...1)

Lecture 12 - Selecting the BEST Regression model (Continued...2)

Lecture 13 - Selecting the BEST Regression model (Continued...3)

Lecture 14 - Multicollinearity

Lecture 15 - Multicollinearity (Continued...1)

Lecture 16 - Multicollinearity (Continued...2)

Lecture 17 - Model Adequacy Checking

Lecture 18 - Model Adequacy Checking (Continued...1)

Lecture 19 - Model Adequacy Checking (Continued...2)

Lecture 20 - Test for Influential Observations

Lecture 21 - Transformations and Weighting to correct model inadequacies

Lecture 22 - Transformations and Weighting to correct model inadequacies (Continued...1)

Lecture 23 - Transformations and Weighting to correct model inadequacies (Continued...2)

Lecture 24 - Dummy Variables

Lecture 25 - Dummy Variables (Continued...1)

Lecture 26 - Dummy Variables (Continued...2)

Lecture 27 - Polynomial Regression Models

Lecture 28 - Polynomial Regression Models (Continued...1)

Lecture 29 - Polynomial Regression Models (Continued...2)

Lecture 30 - Generalized Linear Models

Lecture 31 - Generalized Linear Models (Continued.)

[Lecture 32 - Non-Linear Estimation](#)

[Lecture 33 - Regression Models with Autocorrelated Errors](#)

[Lecture 34 - Regression Models with Autocorrelated Errors \(Continued.\)](#)

[Lecture 35 - Measurement Errors & Calibration Problem](#)

[Lecture 36 - Tutorial - I](#)

[Lecture 37 - Tutorial - II](#)

[Lecture 38 - Tutorial - III](#)

[Lecture 39 - Tutorial - IV](#)

[Lecture 40 - Tutorial - V](#)

Lecture 1 - Introduction and Motivation

Lecture 2 - Basic Concepts of Point Estimations - I

Lecture 3 - Basic Concepts of Point Estimations - II

Lecture 4 - Finding Estimators - I

Lecture 5 - Finding Estimators - II

Lecture 6 - Finding Estimators - III

Lecture 7 - Properties of MLEs

Lecture 8 - Lower Bounds for Variance - I

Lecture 9 - Lower Bounds for Variance - II

Lecture 10 - Lower Bounds for Variance - III

Lecture 11 - Lower Bounds for Variance - IV

Lecture 12 - Sufficiency

Lecture 13 - Sufficiency and Information

Lecture 14 - Minimal Sufficiency, Completeness

Lecture 15 - UMVU Estimation, Ancillarity

Lecture 16 - Invariance - I

Lecture 17 - Invariance - II

Lecture 18 - Bayes and Minimax Estimation - I

Lecture 19 - Bayes and Minimax Estimation - II

Lecture 20 - Bayes and Minimax Estimation - III

Lecture 21 - Testing of Hypotheses : Basic Concepts

Lecture 22 - Neyman Pearson Fundamental Lemma

Lecture 23 - Applications of NP lemma

Lecture 24 - UMP Tests

Lecture 25 - UMP Tests (Continued.)

Lecture 26 - UMP Unbiased Tests

Lecture 27 - UMP Unbiased Tests (Continued.)

Lecture 28 - UMP Unbiased Tests : Applications

Lecture 29 - Unbiased Tests for Normal Populations

Lecture 30 - Unbiased Tests for Normal Populations (Continued.)

Lecture 31 - Likelihood Ratio Tests - I

[Lecture 32 - Likelihood Ratio Tests - II](#)

[Lecture 33 - Likelihood Ratio Tests - III](#)

[Lecture 34 - Likelihood Ratio Tests - IV](#)

[Lecture 35 - Invariant Tests](#)

[Lecture 36 - Test for Goodness of Fit](#)

[Lecture 37 - Sequential Procedure](#)

[Lecture 38 - Sequential Procedure \(Continued.\)](#)

[Lecture 39 - Confidence Intervals](#)

[Lecture 40 - Confidence Intervals \(Continued.\)](#)

Lecture 1 - Rational Numbers and Rational Cuts

Lecture 2 - Irrational numbers, Dedekind's Theorem

Lecture 3 - Continuum and Exercises

Lecture 4 - Continuum and Exercises (Continued.)

Lecture 5 - Cantor's Theory of Irrational Numbers

Lecture 6 - Cantor's Theory of Irrational Numbers (Continued.)

Lecture 7 - Equivalence of Dedekind and Cantor's Theory

Lecture 8 - Finite, Infinite, Countable and Uncountable Sets of Real Numbers

Lecture 9 - Types of Sets with Examples, Metric Space

Lecture 10 - Various properties of open set, closure of a set

Lecture 11 - Ordered set, Least upper bound, greatest lower bound of a set

Lecture 12 - Compact Sets and its properties

Lecture 13 - Weiersstrass Theorem, Heine Borel Theorem, Connected set

Lecture 14 - Tutorial - II

Lecture 15 - Concept of limit of a sequence

Lecture 16 - Some Important limits, Ratio tests for sequences of Real Numbers

Lecture 17 - Cauchy theorems on limit of sequences with examples

Lecture 18 - Fundamental theorems on limits, Bolzano-Weiersstrass Theorem

Lecture 19 - Theorems on Convergent and divergent sequences

Lecture 20 - Cauchy sequence and its properties

Lecture 21 - Infinite series of real numbers

Lecture 22 - Comparison tests for series, Absolutely convergent and Conditional convergent series

Lecture 23 - Tests for absolutely convergent series

Lecture 24 - Raabe's test, limit of functions, Cluster point

Lecture 25 - Some results on limit of functions

Lecture 26 - Limit Theorems for functions

Lecture 27 - Extension of limit concept (one sided limits)

Lecture 28 - Continuity of Functions

Lecture 29 - Properties of Continuous Functions

Lecture 30 - Boundedness Theorem, Max-Min Theorem and Bolzano's theorem

Lecture 31 - Uniform Continuity and Absolute Continuity

- Lecture 32 - Types of Discontinuities, Continuity and Compactness
- Lecture 33 - Continuity and Compactness (Continued.), Connectedness
- Lecture 34 - Differentiability of real valued function, Mean Value Theorem
- Lecture 35 - Mean Value Theorem (Continued.)
- Lecture 36 - Application of MVT , Darboux Theorem, L Hospital Rule
- Lecture 37 - L'Hospital Rule and Taylor's Theorem
- Lecture 38 - Tutorial - III
- Lecture 39 - Riemann/Riemann Stieltjes Integral
- Lecture 40 - Existence of Reimann Stieltjes Integral
- Lecture 41 - Properties of Reimann Stieltjes Integral
- Lecture 42 - Properties of Reimann Stieltjes Integral (Continued.)
- Lecture 43 - Definite and Indefinite Integral
- Lecture 44 - Fundamental Theorems of Integral Calculus
- Lecture 45 - Improper Integrals
- Lecture 46 - Convergence Test for Improper Integrals

[Lecture 1 - Foundations of Probability](#)

[Lecture 2 - Laws of Probability](#)

[Lecture 3 - Random Variables](#)

[Lecture 4 - Moments and Special Distributions](#)

[Lecture 5 - Moments and Special Distributions \(Continued...\)](#)

[Lecture 6 - Special Distributions \(Continued...\)](#)

[Lecture 7 - Special Distributions \(Continued...\)](#)

[Lecture 8 - Sampling Distributions](#)

[Lecture 9 - Parametric Methods - I](#)

[Lecture 10 - Parametric Methods - II](#)

[Lecture 11 - Parametric Methods - III](#)

[Lecture 12 - Parametric Methods - IV](#)

[Lecture 13 - Parametric Methods - V](#)

[Lecture 14 - Parametric Methods - VI](#)

[Lecture 15 - Parametric Methods - VII](#)

[Lecture 16 - Multivariate Analysis - I](#)

[Lecture 17 - Multivariate Analysis - II](#)

[Lecture 18 - Multivariate Analysis - III](#)

[Lecture 19 - Multivariate Analysis - IV](#)

[Lecture 20 - Multivariate Analysis - V](#)

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[Lecture 25 - Multivariate Analysis - X](#)

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[Lecture 28 - Non parametric Methods - I](#)

[Lecture 29 - Non parametric Methods - II](#)

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[Lecture 31 - Non parametric Methods - IV](#)

[Lecture 32 - Nonparametric Methods - V](#)

[Lecture 33 - Nonparametric Methods - VI](#)

[Lecture 34 - Nonparametric Methods - VII](#)

[Lecture 35 - Nonparametric Methods - VIII](#)

[Lecture 36 - Nonparametric Methods - IX](#)

[Lecture 37 - Nonparametric Methods - X](#)

[Lecture 38 - Nonparametric Methods - XI](#)

[Lecture 39 - Nonparametric Methods - XII](#)

[Lecture 40 - Nonparametric Methods - XIII](#)

Lecture 1 - Sets, Classes, Collection

Lecture 2 - Sequence of Sets

Lecture 3 - Ring, Field (Algebra)

Lecture 4 - Sigma-Ring, Sigma-Field, Monotone Class

Lecture 5 - Random Experiment, Events

Lecture 6 - Definitions of Probability

Lecture 7 - Properties of Probability Function - I

Lecture 8 - Properties of Probability Function - II

Lecture 9 - Conditional Probability

Lecture 10 - Independence of Events

Lecture 11 - Problems in Probability - I

Lecture 12 - Problems in Probability - II

Lecture 13 - Random Variables

Lecture 14 - Probability Distribution of a Random Variable - I

Lecture 15 - Probability Distribution of a Random Variable - II

Lecture 16 - Moments

Lecture 17 - Characteristics of Distributions - I

Lecture 18 - Characteristics of Distributions - II

Lecture 19 - Special Discrete Distributions - I

Lecture 20 - Special Discrete Distributions - II

Lecture 21 - Special Discrete Distributions - III

Lecture 22 - Poisson Process - I

Lecture 23 - Poisson Process - II

Lecture 24 - Special Continuous Distributions - I

Lecture 25 - Special Continuous Distributions - II

Lecture 26 - Special Continuous Distributions - III

Lecture 27 - Special Continuous Distributions - IV

Lecture 28 - Special Continuous Distributions - V

Lecture 29 - Normal Distribution

Lecture 30 - Problems on Normal Distribution

Lecture 31 - Problems on Special Distributions - I

- Lecture 32 - Problems on Special Distributions - II
- Lecture 33 - Function of a random variable - I
- Lecture 34 - Function of a random variable - II
- Lecture 35 - Joint Distributions - I
- Lecture 36 - Joint Distributions - II
- Lecture 37 - Independence, Product Moments
- Lecture 38 - Linearity Property of Correlation and Examples
- Lecture 39 - Bivariate Normal Distribution - I
- Lecture 40 - Bivariate Normal Distribution - II
- Lecture 41 - Additive Properties of Distributions - I
- Lecture 42 - Additive Properties of Distributions - II
- Lecture 43 - Transformation of Random Variables
- Lecture 44 - Distribution of Order Statistics
- Lecture 45 - Basic Concepts
- Lecture 46 - Chi-Square Distribution
- Lecture 47 - Chi-Square Distribution (Continued...), t-Distribution
- Lecture 48 - F-Distribution
- Lecture 49 - Descriptive Statistics - I
- Lecture 50 - Descriptive Statistics - II
- Lecture 51 - Descriptive Statistics - III
- Lecture 52 - Descriptive Statistics - IV
- Lecture 53 - Introduction to Estimation
- Lecture 54 - Unbiased and Consistent Estimators
- Lecture 55 - LSE, MME
- Lecture 56 - Examples on MME, MLE
- Lecture 57 - Examples on MLE - I
- Lecture 58 - Examples on MLE - II, MSE
- Lecture 59 - UMVUE, Sufficiency, Completeness
- Lecture 60 - Rao - Blackwell Theorem and Its Applications
- Lecture 61 - Confidence Intervals - I
- Lecture 62 - Confidence Intervals - II
- Lecture 63 - Confidence Intervals - III
- Lecture 64 - Confidence Intervals - IV

[Lecture 65 - Basic Definitions](#)

[Lecture 66 - Two Types of Errors](#)

[Lecture 67 - Neyman-Pearson Fundamental Lemma](#)

[Lecture 68 - Applications of N-P Lemma - I](#)

[Lecture 69 - Applications of N-P Lemma - II](#)

[Lecture 70 - Testing for Normal Mean](#)

[Lecture 71 - Testing for Normal Variance](#)

[Lecture 72 - Large Sample Test for Variance and Two Sample Problem](#)

[Lecture 73 - Paired t-Test](#)

[Lecture 74 - Examples](#)

[Lecture 75 - Testing Equality of Proportions](#)

[Lecture 76 - Chi-Square Test for Goodness Fit - I](#)

[Lecture 77 - Chi-Square Test for Goodness Fit - II](#)

[Lecture 78 - Testing for Independence in rxc Contingency Table - I](#)

[Lecture 79 - Testing for Independence in rxc Contingency Table - II](#)

Lecture 1 - Introduction to Multivariate Statistical Modeling

Lecture 2 - Introduction to Multivariate Statistical Modeling: Data types, models, and modeling

Lecture 3 - Statistical approaches to model building

Lecture 4 - Statistical approaches to model building (Continued...)

Lecture 5 - Univariate Descriptive Statistics

Lecture 6 - Univariate Descriptive Statistics (Continued...)

Lecture 7 - Normal Distribution and Chi-squared Distribution

Lecture 8 - t-distribution, F-distribution, and Central Limit Theorem

Lecture 9 - Univariate Inferential Statistics: Estimation

Lecture 10 - Univariate Inferential Statistics: Estimation (Continued...)

Lecture 11 - Univariate Inferential Statistics: Hypothesis Testing

Lecture 12 - Hypothesis Testing (Continued...): Decision Making Scenarios

Lecture 13 - Multivariate Descriptive Statistics: Mean Vector

Lecture 14 - Multivariate Descriptive Statistics: Covariance Matrix

Lecture 15 - Multivariate Descriptive Statistics: Correlation Matrix

Lecture 16 - Multivariate Descriptive Statistics: Relationship between correlation and covariance matrices

Lecture 17 - Multivariate Normal Distribution

Lecture 18 - Multivariate Normal Distribution (Continued...)

Lecture 19 - Multivariate Normal Distribution (Continued...): Geometrical Interpretation

Lecture 20 - Multivariate Normal Distribution (Continued...): Examining data for multivariate normal distribution

Lecture 21 - Multivariate Inferential Statistics: Basics and Hotelling T-square statistic

Lecture 22 - Multivariate Inferential Statistics: Confidence Region

Lecture 23 - Multivariate Inferential Statistics: Simultaneous confidence interval and Hypothesis testing

Lecture 24 - Multivariate Inferential Statistics: Hypothesis testing for equality of two population mean vectors

Lecture 25 - Analysis of Variance (ANOVA)

Lecture 26 - Analysis of Variance (ANOVA): Decomposition of Total sum of squares

Lecture 27 - Analysis of Variance (ANOVA): Estimation of Parameters and Model Adequacy tests

Lecture 28 - Two-way and Three-way Analysis of Variance (ANOVA)

Lecture 29 - Tutorial ANOVA

Lecture 30 - Tutorial ANOVA (Continued...)

Lecture 31 - Multivariate Analysis of Variance (MANOVA): Conceptual Model

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- Lecture 32 - Multivariate Analysis of Variance (MANOVA): Assumptions and Decomposition of total sum square and cross products (SSCP)
- Lecture 33 - Multivariate Analysis of Variance (MANOVA): Decomposition of total sum square and cross products (SSCP) (Continued...)
- Lecture 34 - Multivariate Analysis of Variance (MANOVA): Estimation and Hypothesis testing
- Lecture 35 - MANOVA Case Study
- Lecture 36 - Multiple Linear Regression: Introduction
- Lecture 37 - Multiple Linear Regression: Assumptions and Estimation of model parameters
- Lecture 38 - Multiple Linear Regression: Sampling Distribution of parameter estimates
- Lecture 39 - Multiple Linear Regression: Sampling Distribution of parameter estimates (Continued...)
- Lecture 40 - Multiple Linear Regression: Model Adequacy Tests
- Lecture 41 - Multiple Linear Regression: Model Adequacy Tests (Continued...)
- Lecture 42 - Multiple Linear Regression: Test of Assumptions
- Lecture 43 - MLR-Model diagnostics
- Lecture 44 - MLR-case study
- Lecture 45 - Multivariate Linear Regression: Conceptual model and assumptions
- Lecture 46 - Multivariate Linear Regression: Estimation of parameters
- Lecture 47 - Multivariate Linear Regression: Estimation of parameters (Continued...)
- Lecture 48 - Multiple Linear Regression: Sampling Distribution of parameter estimates
- Lecture 49 - Multivariate Linear Regression: Model Adequacy Tests
- Lecture 50 - Multiple Linear Regression: Model Adequacy Tests (Continued...)
- Lecture 51 - Regression modeling using SPSS
- Lecture 52 - Principal Component Analysis (PCA): Conceptual Model
- Lecture 53 - Principal Component Analysis (PCA): Extraction of Principal components (PCs)
- Lecture 54 - Principal Component Analysis (PCA): Model Adequacy and Interpretation
- Lecture 55 - Principal Component Analysis (PCA): Model Adequacy and Interpretation (Continued...)
- Lecture 56 - Factor Analysis: Basics and Orthogonal factor models
- Lecture 57 - Factor Analysis: Types of models and key questions
- Lecture 58 - Factor Analysis: Parameter Estimation
- Lecture 59 - Factor Analysis: Parameter Estimation (Continued...)
- Lecture 60 - Factor Analysis: Model Adequacy tests and factor rotation
- Lecture 61 - Factor Analysis: Factor scores and case study

Lecture 1 - Introduction to PDE

Lecture 2 - Classification of PDE

Lecture 3 - Principle of Linear Superposition

Lecture 4 - Standard Eigen Value Problem and Special ODEs

Lecture 5 - Adjoint Operator

Lecture 6 - Generalized Sturm - Liouville Problem

Lecture 7 - Properties of Adjoint Operator

Lecture 8 - Separation of Variables: Rectangular Coordinate Systems

Lecture 9 - Solution of 3 Dimensional Parabolic Problem

Lecture 10 - Solution of 4 Dimensional Parabolic problem

Lecture 11 - Solution of 4 Dimensional Parabolic Problem (Continued...)

Lecture 12 - Solution of Elliptical PDE

Lecture 13 - Solution of Hyperbolic PDE

Lecture 14 - Orthogonality of Bessel Function and 2 Dimensional Cylindrical Coordinate System

Lecture 15 - Cylindrical Co-ordinate System - 3 Dimensional Problem

Lecture 16 - Spherical Polar Coordinate System

Lecture 17 - Spherical Polar Coordinate System (Continued...)

Lecture 18 - Example of Generalized 3 Dimensional Problem

Lecture 19 - Example of Application Oriented Problems

Lecture 20 - Examples of Application Oriented Problems (Continued...)

Lecture 1 - Countable and Uncountable sets

Lecture 2 - Properties of Countable and Uncountable sets

Lecture 3 - Examples of Countable and Uncountable sets

Lecture 4 - Concepts of Metric Space

Lecture 5 - Open ball, Closed ball, Limit point of a set

Lecture 6 - Tutorial-I

Lecture 7 - Some theorems on Open and Closed sets

Lecture 8 - Ordered set, Least upper bound, Greatest lower bound of a set

Lecture 9 - Ordered set, Least upper bound, Greatest lower bound of a set (Continued...)

Lecture 10 - Compact Set

Lecture 11 - Properties of Compact sets

Lecture 12 - Tutorial-II

Lecture 13 - Heine Borel Theorem

Lecture 14 - Weierstrass Theorem

Lecture 15 - Cantor set and its properties

Lecture 16 - Derived set and Dense set

Lecture 17 - Limit of a sequence and monotone sequence

Lecture 18 - Tutorial-III

Lecture 19 - Some Important limits of sequences

Lecture 20 - Ratio Test Cauchy's theorems on limits of sequences of real numbers

Lecture 21 - Fundamental theorems on limits

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Lecture 10 - Subspaces (Continued...), Spanning Sets, Linear Independence, Dependence

Lecture 11 - Basis for a vector space

Lecture 12 - Dimension of a vector space

Lecture 13 - Dimensions of Sums of Subspaces

Lecture 14 - Linear Transformations

Lecture 15 - The Null Space and the Range Space of a Linear Transformation

Lecture 16 - The Rank-Nullity-Dimension Theorem. Isomorphisms Between Vector Spaces

Lecture 17 - Isomorphic Vector Spaces, Equality of the Row-rank and the Column-rank - I

Lecture 18 - Equality of the Row-rank and the Column-rank - II

Lecture 19 - The Matrix of a Linear Transformation

Lecture 20 - Matrix for the Composition and the Inverse. Similarity Transformation

Lecture 21 - Linear Functionals. The Dual Space. Dual Basis - I

Lecture 22 - Dual Basis II. Subspace Annihilators - I

Lecture 23 - Subspace Annihilators - II

Lecture 24 - The Double Dual. The Double Annihilator

Lecture 25 - The Transpose of a Linear Transformation. Matrices of a Linear Transformation and its Transpose

Lecture 26 - Eigenvalues and Eigenvectors of Linear Operators

Lecture 27 - Diagonalization of Linear Operators. A Characterization

Lecture 28 - The Minimal Polynomial

Lecture 29 - The Cayley-Hamilton Theorem

Lecture 30 - Invariant Subspaces

[Lecture 31 - Triangulability, Diagonalization in Terms of the Minimal Polynomial](#)

[Lecture 32 - Independent Subspaces and Projection Operators](#)

[Lecture 33 - Direct Sum Decompositions and Projection Operators - I](#)

[Lecture 34 - Direct Sum Decompositions and Projection Operators - II](#)

[Lecture 35 - The Primary Decomposition Theorem and Jordan Decomposition](#)

[Lecture 36 - Cyclic Subspaces and Annihilators](#)

[Lecture 37 - The Cyclic Decomposition Theorem - I](#)

[Lecture 38 - The Cyclic Decomposition Theorem - II. The Rational Form](#)

[Lecture 39 - Inner Product Spaces](#)

[Lecture 40 - Norms on Vector spaces. The Gram-Schmidt Procedure I](#)

[Lecture 41 - The Gram-Schmidt Procedure II. The QR Decomposition](#)

[Lecture 42 - Bessel's Inequality, Parseval's Identity, Best Approximation](#)

[Lecture 43 - Best Approximation: Least Squares Solutions](#)

[Lecture 44 - Orthogonal Complementary Subspaces, Orthogonal Projections](#)

[Lecture 45 - Projection Theorem. Linear Functionals](#)

[Lecture 46 - The Adjoint Operator](#)

[Lecture 47 - Properties of the Adjoint Operation. Inner Product Space Isomorphism](#)

[Lecture 48 - Unitary Operators](#)

[Lecture 49 - Unitary operators - II. Self-Adjoint Operators - I.](#)

[Lecture 50 - Self-Adjoint Operators - II - Spectral Theorem](#)

[Lecture 51 - Normal Operators - Spectral Theorem](#)

NPTEL : Mathematical Logic (Mathematics)

Co-ordinators : Prof. Arindama Singh

Lecture 1 - Sets and Strings

Lecture 2 - Syntax of Propositional Logic

Lecture 3 - Unique Parsing

Lecture 4 - Semantics of PL

Lecture 5 - Consequences and Equivalences

Lecture 6 - Five results about PL

Lecture 7 - Calculations and Informal Proofs

Lecture 8 - More Informal Proofs

Lecture 9 - Normal forms

Lecture 10 - SAT and 3SAT

Lecture 11 - Horn-SAT and Resolution

Lecture 12 - Resolution

Lecture 13 - Adequacy of Resolution

Lecture 14 - Adequacy and Resolution Strategies

Lecture 15 - Propositional Calculus (PC)

Lecture 16 - Some Results about PC

Lecture 17 - Arguing with Proofs

Lecture 18 - Adequacy of PC

Lecture 19 - Compactness & Analytic Tableau

Lecture 20 - Examples of Tableau Proofs

Lecture 21 - Adequacy of Tableaux

Lecture 22 - Syntax of First order Logic (FL)

Lecture 23 - Symbolization & Scope of Quantifiers

Lecture 24 - Hurdles in giving Meaning

Lecture 25 - Semantics of FL

Lecture 26 - Relevance Lemma

Lecture 27 - Validity, Satisfiability & Equivalence

Lecture 28 - Six Results about FL

Lecture 29 - Laws, Calculation & Informal Proof

Lecture 30 - Quantifier Laws and Consequences

Lecture 31 - More Proofs and Prenex Form

[Lecture 32 - Prenex Form Conversion](#)

[Lecture 33 - Skolem Form](#)

[Lecture 34 - Syntactic Interpretation](#)

[Lecture 35 - Herbrand's Theorem](#)

[Lecture 36 - Most General Unifiers](#)

[Lecture 37 - Resolution Rules](#)

[Lecture 38 - Resolution Examples](#)

[Lecture 39 - Ariomatic System FC](#)

[Lecture 40 - FC and Semidecidability of FL](#)

[Lecture 41 - Analytic Tableau for FL](#)

[Lecture 42 - Godels Incompleteness Theorems](#)

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Lecture 2 - Functions and Relations

Lecture 3 - Finite and Infinite Sets

Lecture 4 - Countable Sets

Lecture 5 - Uncountable Sets, Cardinal Number

Lecture 6 - Real Number System

Lecture 7 - LUB Axiom

Lecture 8 - Sequences of Real Numbers

Lecture 9 - Sequences of Real Numbers - (Continued.)

Lecture 10 - Sequences of Real Numbers - (Continued.)

Lecture 11 - Infinite Series of Real Numbers

Lecture 12 - Series of nonnegative Real Numbers

Lecture 13 - Conditional Convergence

Lecture 14 - Metric Spaces: Definition and Examples

Lecture 15 - Metric Spaces: Examples and Elementary Concepts

Lecture 16 - Balls and Spheres

Lecture 17 - Open Sets

Lecture 18 - Closure Points, Limit Points and isolated Points

Lecture 19 - Closed sets

Lecture 20 - Sequences in Metric Spaces

Lecture 21 - Completeness

Lecture 22 - Baire Category Theorem

Lecture 23 - Limit and Continuity of a Function defined on a Metric space

Lecture 24 - Continuous Functions on a Metric Space

Lecture 25 - Uniform Continuity

Lecture 26 - Connectedness

Lecture 27 - Connected Sets

Lecture 28 - Compactness

Lecture 29 - Compactness (Continued.)

Lecture 30 - Characterizations of Compact Sets

Lecture 31 - Continuous Functions on Compact Sets

[Lecture 32 - Types of Discontinuity](#)

[Lecture 33 - Differentiation](#)

[Lecture 34 - Mean Value Theorems](#)

[Lecture 35 - Mean Value Theorems \(Continued.\)](#)

[Lecture 36 - Taylor's Theorem](#)

[Lecture 37 - Differentiation of Vector Valued Functions](#)

[Lecture 38 - Integration](#)

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[Lecture 41 - Integrable Functions \(Continued.\)](#)

[Lecture 42 - Integration as a Limit of Sum](#)

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[Lecture 44 - Integration of Vector Valued Functions](#)

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[Lecture 46 - Sequences and Series of Functions](#)

[Lecture 47 - Uniform Convergence](#)

[Lecture 48 - Uniform Convergence and Integration](#)

[Lecture 49 - Uniform Convergence and Differentiation](#)

[Lecture 50 - Construction of Everywhere Continuous Nowhere Differentiable Function](#)

[Lecture 51 - Approximation of a Continuous Function by Polynomials: Weierstrass Theorem](#)

[Lecture 52 - Equicontinuous family of Functions: Arzela - Ascoli Theorem](#)

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Lecture 2 - Data Mining, Data assimilation and prediction

Lecture 3 - A classification of forecast errors

Lecture 4 - Finite Dimensional Vector Space

Lecture 5 - Matrices

Lecture 6 - Matrices (Continued...)

Lecture 7 - Multi-variate Calculus

Lecture 8 - Optimization in Finite Dimensional Vector spaces

Lecture 9 - Deterministic, Static, linear Inverse (well-posed) Problems

Lecture 10 - Deterministic, Static, Linear Inverse (Ill-posed) Problems

Lecture 11 - A Geometric View \hat{A} - Projections

Lecture 12 - Deterministic, Static, nonlinear Inverse Problems

Lecture 13 - On-line Least Squares

Lecture 14 - Examples of static inverse problems

Lecture 15 - Interlude and a Way Forward

Lecture 16 - Matrix Decomposition Algorithms

Lecture 17 - Matrix Decomposition Algorithms (Continued...)

Lecture 18 - Minimization algorithms

Lecture 19 - Minimization algorithms (Continued...)

Lecture 20 - Inverse problems in deterministic

Lecture 21 - Inverse problems in deterministic (Continued...)

Lecture 22 - Forward sensitivity method

Lecture 23 - Relation between FSM and 4DVAR

Lecture 24 - Statistical Estimation

Lecture 25 - Statistical Least Squares

Lecture 26 - Maximum Likelihood Method

Lecture 27 - Bayesian Estimation

Lecture 28 - From Gauss to Kalman-Linear Minimum Variance Estimation

Lecture 29 - Initialization Classical Method

Lecture 30 - Optimal interpolations

Lecture 31 - A Bayesian Formation-3D-VAR methods

[Lecture 32 - Linear Stochastic Dynamics - Kalman Filter](#)

[Lecture 33 - Linear Stochastic Dynamics - Kalman Filter \(Continued...\)](#)

[Lecture 34 - Linear Stochastic Dynamics - Kalman Filter \(Continued...\)](#)

[Lecture 35 - Covariance Square Root Filter](#)

[Lecture 36 - Nonlinear Filtering](#)

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[Lecture 39 - Deterministic predictability](#)

[Lecture 40 - Predictability A stochastic view and Summary](#)

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Lecture 2 - Long division

Lecture 3 - Applications of Long division

Lecture 4 - Lagrange interpolation

Lecture 5 - The 0-1 idea in other contexts - dot and cross product

Lecture 6 - Taylors formula

Lecture 7 - The Chebyshev polynomials

Lecture 8 - Counting number of monomials - several variables

Lecture 9 - Permutations, combinations and the binomial theorem

Lecture 10 - Combinations with repetition, and counting monomials

Lecture 11 - Combinations with restrictions, recurrence relations

Lecture 12 - Fibonacci numbers; an identity and a bijective proof

Lecture 13 - Permutations and cycle type

Lecture 14 - The sign of a permutation, composition of permutations

Lecture 15 - Rules for drawing tangle diagrams

Lecture 16 - Signs and cycle decompositions

Lecture 17 - Sorting lists of numbers, and crossings in tangle diagrams

Lecture 18 - Real and integer valued polynomials

Lecture 19 - Integer valued polynomials revisited

Lecture 20 - Functions on the real line, continuity

Lecture 21 - The intermediate value property

Lecture 22 - Visualizing functions

Lecture 23 - Functions on the plane, Rigid motions

Lecture 24 - More examples of functions on the plane, dilations

Lecture 25 - Composition of functions

Lecture 26 - Affine and Linear transformations

Lecture 27 - Length and Area dilation, the derivative

Lecture 28 - Examples-I

Lecture 29 - Examples-II

Lecture 30 - Linear equations, Lagrange interpolation revisited

Lecture 31 - Completed Matrices in combinatorics

[Lecture 32 - Polynomials acting on matrices](#)

[Lecture 33 - Divisibility, prime numbers](#)

[Lecture 34 - Congruences, Modular arithmetic](#)

[Lecture 35 - The Chinese remainder theorem](#)

[Lecture 36 - The Euclidean algorithm, the 0-1 idea and the Chinese remainder theorem](#)

Lecture 1 - Fundamental Theorems Connected with Zeros of Analytic Functions

Lecture 2 - The Argument (Counting) Principle, Rouché's Theorem and The Fundamental Theorem of Algebra

Lecture 3 - Morera's Theorem and Normal Limits of Analytic Functions

Lecture 4 - Hurwitz's Theorem and Normal Limits of Univalent Functions

Lecture 5 - Local Constancy of Multiplicities of Assumed Values

Lecture 6 - The Open Mapping Theorem

Lecture 7 - Introduction to the Inverse Function Theorem

Lecture 8 - Completion of the Proof of the Inverse Function Theorem: The Integral Inversion Formula for the Inverse Function

Lecture 9 - Univalent Analytic Functions have never-zero Derivatives and are Analytic Isomorphisms

Lecture 10 - Introduction to the Implicit Function Theorem

Lecture 11 - Proof of the Implicit Function Theorem: Topological Preliminaries

Lecture 12 - Proof of the Implicit Function Theorem: The Integral Formula for & Analyticity of the Explicit Function

Lecture 13 - Doing Complex Analysis on a Real Surface: The Idea of a Riemann Surface

Lecture 14 - $F(z,w)=0$ is naturally a Riemann Surface

Lecture 15 - Constructing the Riemann Surface for the Complex Logarithm

Lecture 16 - Constructing the Riemann Surface for the m -th root function

Lecture 17 - The Riemann Surface for the functional inverse of an analytic mapping at a critical point

Lecture 18 - The Algebraic nature of the functional inverses of an analytic mapping at a critical point

Lecture 19 - The Idea of a Direct Analytic Continuation or an Analytic Extension

Lecture 20 - General or Indirect Analytic Continuation and the Lipschitz Nature of the Radius of Convergence

Lecture 21 - Analytic Continuation Along Paths via Power Series Part A

Lecture 22 - Analytic Continuation Along Paths via Power Series Part B

Lecture 23 - Continuity of Coefficients occurring in Families of Power Series defining Analytic Continuations along Paths

Lecture 24 - Analytic Continuability along Paths: Dependence on the Initial Function and on the Path - First Version of the Monodromy Theorem

Lecture 25 - Maximal Domains of Direct and Indirect Analytic Continuation: Second Version of the Monodromy Theorem

Lecture 26 - Deducing the Second (Simply Connected) Version of the Monodromy Theorem from the First (Homotopy) Version

Lecture 27 - Existence and Uniqueness of Analytic Continuations on Nearby Paths

Lecture 28 - Proof of the First (Homotopy) Version of the Monodromy Theorem

Lecture 29 - Proof of the Algebraic Nature of Analytic Branches of the Functional Inverse of an Analytic Function at a Critical Point

Lecture 30 - The Mean-Value Property, Harmonic Functions and the Maximum Principle

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[Lecture 31 - Proofs of Maximum Principles and Introduction to Schwarz Lemma](#)

[Lecture 32 - Proof of Schwarz Lemma and Uniqueness of Riemann Mappings](#)

[Lecture 33 - Reducing Existence of Riemann Mappings to Hyperbolic Geometry of Sub-domains of the Unit Disc](#)

[Lecture 34 - Differential or Infinitesimal Schwarz Lemma, Picks Lemma, Hyperbolic Arclengths, Metric and Geodesics on the Unit Disc](#)

[Lecture 35 - Differential or Infinitesimal Schwarz Lemma, Picks Lemma, Hyperbolic Arclengths, Metric and Geodesics on the Unit Disc](#)

[Lecture 36 - Hyperbolic Geodesics for the Hyperbolic Metric on the Unit Disc](#)

[Lecture 37 - Schwarz-Pick Lemma for the Hyperbolic Metric on the Unit Disc](#)

[Lecture 38 - Arzela-Ascoli Theorem: Under Uniform Boundedness, Equicontinuity and Uniform Sequential Compactness are Equivalent](#)

[Lecture 39 - Completion of the Proof of the Arzela-Ascoli Theorem and Introduction to Montels Theorem](#)

[Lecture 40 - The Proof of Montels Theorem](#)

[Lecture 41 - The Candidate for a Riemann Mapping](#)

[Lecture 42 - Completion of Proof of The Riemann Mapping Theorem](#)

[Lecture 43 - Completion of Proof of The Riemann Mapping Theorem](#)

Lecture 1 - Course Introduction

Lecture 2 - Sets, Relations and Functions

Lecture 3 - Propositional Logic and Predicate Logic

Lecture 4 - Propositional Logic and Predicate Logic (Part 2)

Lecture 5 - Elementary Number Theory

Lecture 6 - Formal Proofs

Lecture 7 - Direct Proofs

Lecture 8 - Case Study

Lecture 9 - Case Study (Part 2)

Lecture 10 - Sets, Relations, Function and Logic

Lecture 11 - Proof by Contradiction (Part 1)

Lecture 12 - Proof by Contradiction (Part 2)

Lecture 13 - Proof by Contraposition

Lecture 14 - Proof by Counter Example

Lecture 15 - Mathematical Induction (Part 1)

Lecture 16 - Mathematical Induction (Part 2)

Lecture 17 - Mathematical Induction (Part 3)

Lecture 18 - Mathematical Induction (Part 4)

Lecture 19 - Mathematical Induction (Part 5)

Lecture 20 - Mathematical Induction (Part 6)

Lecture 21 - Mathematical Induction (Part 7)

Lecture 22 - Mathematical Induction (Part 8)

Lecture 23 - Introduction to Graph Theory

Lecture 24 - Handshake Problem

Lecture 25 - Tournament Problem

Lecture 26 - Tournament Problem (Part 2)

Lecture 27 - Ramsey Problem

Lecture 28 - Ramsey Problem (Part 2)

Lecture 29 - Properties of Graphs

Lecture 30 - Problem 1

Lecture 31 - Problem 2

[Lecture 32 - Problem 3 & 4](#)

[Lecture 33 - Counting for Selection](#)

[Lecture 34 - Counting for Distribution](#)

[Lecture 35 - Counting for Distribution \(Part 2\)](#)

[Lecture 36 - Some Counting Problems](#)

[Lecture 37 - Counting using Recurrence Relations](#)

[Lecture 38 - Counting using Recurrence Relations \(Part 2\)](#)

[Lecture 39 - Solving Recurrence Relations \(Part 1\)](#)

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[Lecture 45 - Generating Functions \(Part 1\)](#)

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[Lecture 47 - Generating Functions \(Part 3\)](#)

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[Lecture 50 - Modeling: Graph Theory and Linear Programming](#)

[Lecture 51 - Combinatorics](#)

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NPTEL : Advanced Complex Analysis - Part 2 (Mathematics)

Co-ordinators : Dr. T.E. Venkata Balaji

Lecture 1 - Properties of the Image of an Analytic Function - Introduction to the Picard Theorems

Lecture 2 - Recalling Singularities of Analytic Functions - Non-isolated and Isolated Removable, Pole and Essential Singularities

Lecture 3 - Recalling Riemann's Theorem on Removable Singularities

Lecture 4 - Casorati-Weierstrass Theorem; Dealing with the Point at Infinity -- Riemann Sphere and Riemann Stereographic Projection

Lecture 5 - Neighborhood of Infinity, Limit at Infinity and Infinity as an Isolated Singularity

Lecture 6 - Studying Infinity - Formulating Epsilon-Delta Definitions for Infinite Limits and Limits at Infinity

Lecture 7 - When is a function analytic at infinity ?

Lecture 8 - Laurent Expansion at Infinity and Riemann's Removable Singularities Theorem for the Point at Infinity

Lecture 9 - The Generalized Liouville Theorem - Little Brother of Little Picard and Analogue of Casorati-Weierstrass; Failure of Cauchy's Theorem at Infinity

Lecture 10 - Morera's Theorem at Infinity, Infinity as a Pole and Behaviour at Infinity of Rational and Meromorphic Functions

Lecture 11 - Residue at Infinity and Introduction to the Residue Theorem for the Extended Complex Plane - Residue Theorem for the Point at Infinity

Lecture 12 - Proofs of Two Avatars of the Residue Theorem for the Extended Complex Plane and Applications of the Residue at Infinity

Lecture 13 - Infinity as an Essential Singularity and Transcendental Entire Functions

Lecture 14 - Meromorphic Functions on the Extended Complex Plane are Precisely Quotients of Polynomials

Lecture 15 - The Ubiquity of Meromorphic Functions - The Nerves of the Geometric Network Bridging Algebra, Analysis and Topology

Lecture 16 - Continuity of Meromorphic Functions at Poles and Topologies of Spaces of Functions

Lecture 17 - Why Normal Convergence, but Not Globally Uniform Convergence, is the Inevitable in Complex Analysis

Lecture 18 - Measuring Distances to Infinity, the Function Infinity and Normal Convergence of Holomorphic Functions in the Spherical Metric

Lecture 19 - The Invariance Under Inversion of the Spherical Metric on the Extended Complex Plane

Lecture 20 - Introduction to Hurwitz's Theorem for Normal Convergence of Holomorphic Functions in the Spherical Metric

Lecture 21 - Completion of Proof of Hurwitz's Theorem for Normal Limits of Analytic Functions in the Spherical Metric

Lecture 22 - Hurwitz's Theorem for Normal Limits of Meromorphic Functions in the Spherical Metric

Lecture 23 - What could the Derivative of a Meromorphic Function Relative to the Spherical Metric Possibly Be ?

Lecture 24 - Defining the Spherical Derivative of a Meromorphic Function

Lecture 25 - Well-definedness of the Spherical Derivative of a Meromorphic Function at a Pole and Inversion-invariance of the Spherical Derivative

Lecture 26 - Topological Preliminaries - Translating Compactness into Boundedness

Lecture 27 - Introduction to the Arzela-Ascoli Theorem - Passing from abstract Compactness to verifiable Equicontinuity

Lecture 28 - Proof of the Arzela-Ascoli Theorem for Functions - Abstract Compactness Implies Equicontinuity

Lecture 29 - Proof of the Arzela-Ascoli Theorem for Functions - Equicontinuity Implies Compactness

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Lecture 30 - Introduction to the Montel Theorem - the Holomorphic Avatar of the Arzela-Ascoli Theorem & Why you get Equicontinuity for Free

Lecture 31 - Completion of Proof of the Montel Theorem - the Holomorphic Avatar of the Arzela-Ascoli Theorem

Lecture 32 - Introduction to Marty's Theorem - the Meromorphic Avatar of the Montel & Arzela-Ascoli Theorems

Lecture 33 - Proof of one direction of Marty's Theorem - the Meromorphic Avatar of the Montel & Arzela-Ascoli Theorems - Normal Uniform Boundedness of Spherical Derivatives Implies Normal Sequential Compactness

Lecture 34 - Proof of the other direction of Marty's Theorem - the Meromorphic Avatar of the Montel & Arzela-Ascoli Theorems - Normal Sequential Compactness Implies Normal Uniform Boundedness of Spherical Derivatives

Lecture 35 - Normal Convergence at Infinity and Hurwitz's Theorems for Normal Limits of Analytic and Meromorphic Functions at Infinity

Lecture 36 - Normal Sequential Compactness, Normal Uniform Boundedness and Montel's & Marty's Theorems at Infinity

Lecture 37 - Local Analysis of Normality and the Zooming Process - Motivation for Zalcman's Lemma

Lecture 38 - Characterizing Normality at a Point by the Zooming Process and the Motivation for Zalcman's Lemma

Lecture 39 - Local Analysis of Normality and the Zooming Process - Motivation for Zalcman's Lemma

Lecture 40 - Montel's Deep Theorem - The Fundamental Criterion for Normality or Fundamental Normality Test based on Omission of Values

Lecture 41 - Proofs of the Great and Little Picard Theorems

Lecture 42 - Royden's Theorem on Normality Based On Growth Of Derivatives

Lecture 43 - Schottky's Theorem - Uniform Boundedness from a Point to a Neighbourhood & Problem Solving Session

Lecture 1 - What is Algebraic Geometry?

Lecture 2 - The Zariski Topology and Affine Space

Lecture 3 - Going back and forth between subsets and ideals

Lecture 4 - Irreducibility in the Zariski Topology

Lecture 5 - Irreducible Closed Subsets Correspond to Ideals Whose Radicals are Prime

Lecture 6 - Understanding the Zariski Topology on the Affine Line; The Noetherian property in Topology and in Algebra

Lecture 7 - Basic Algebraic Geometry : Varieties, Morphisms, Local Rings, Function Fields and Nonsingularity

Lecture 8 - Topological Dimension, Krull Dimension and Heights of Prime Ideals

Lecture 9 - The Ring of Polynomial Functions on an Affine Variety

Lecture 10 - Geometric Hypersurfaces are Precisely Algebraic Hypersurfaces

Lecture 11 - Why Should We Study Affine Coordinate Rings of Functions on Affine Varieties ?

Lecture 12 - Capturing an Affine Variety Topologically From the Maximal Spectrum of its Ring of Functions

Lecture 13 - Analyzing Open Sets and Basic Open Sets for the Zariski Topology

Lecture 14 - The Ring of Functions on a Basic Open Set in the Zariski Topology

Lecture 15 - Quasi-Compactness in the Zariski Topology; Regularity of a Function at a point of an Affine Variety

Lecture 16 - What is a Global Regular Function on a Quasi-Affine Variety?

Lecture 17 - Characterizing Affine Varieties; Defining Morphisms between Affine or Quasi-Affine Varieties

Lecture 18 - Translating Morphisms into Affines as k -Algebra maps and the Grand Hilbert Nullstellensatz

Lecture 19 - Morphisms into an Affine Correspond to k -Algebra Homomorphisms from its Coordinate Ring of Functions

Lecture 20 - The Coordinate Ring of an Affine Variety Determines the Affine Variety and is Intrinsic to it

Lecture 21 - Automorphisms of Affine Spaces and of Polynomial Rings - The Jacobian Conjecture; The Punctured Plane is Not Affine

Lecture 22 - The Various Avatars of Projective n -space

Lecture 23 - Gluing $(n+1)$ copies of Affine n -Space to Produce Projective n -space in Topology, Manifold Theory and Algebraic Geometry; The Key to the Definition of a Homogeneous Ideal

Lecture 24 - Translating Projective Geometry into Graded Rings and Homogeneous Ideals

Lecture 25 - Expanding the Category of Varieties to Include Projective and Quasi-Projective Varieties

Lecture 26 - Translating Homogeneous Localisation into Geometry and Back

Lecture 27 - Adding a Variable is Undone by Homogenous Localization - What is the Geometric Significance of this Algebraic Fact ?

Lecture 28 - Doing Calculus Without Limits in Geometry ?

Lecture 29 - The Birth of Local Rings in Geometry and in Algebra

Lecture 30 - The Formula for the Local Ring at a Point of a Projective Variety Or Playing with Localisations, Quotients, Homogenisation and Dehomogenisation !

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[Lecture 31 - The Field of Rational Functions or Function Field of a Variety - The Local Ring at the Generic Point](#)

[Lecture 32 - Fields of Rational Functions or Function Fields of Affine and Projective Varieties and their Relationships with Dimensions](#)

[Lecture 33 - Global Regular Functions on Projective Varieties are Simply the Constants](#)

[Lecture 34 - The \$d\$ -uple Embedding and the Non-Intrinsic Nature of the Homogeneous Coordinate Ring of a Projective Variety](#)

[Lecture 35 - The Importance of Local Rings - A Morphism is an Isomorphism if it is a Homeomorphism and Induces Isomorphisms at the Level of Local Rings](#)

[Lecture 36 - The Importance of Local Rings - A Rational Function in Every Local Ring is Globally Regular](#)

[Lecture 37 - Geometric Meaning of Isomorphism of Local Rings - Local Rings are Almost Global](#)

[Lecture 38 - Local Ring Isomorphism, Equals Function Field Isomorphism, Equals Birationality](#)

[Lecture 39 - Why Local Rings Provide Calculus Without Limits for Algebraic Geometry Pun Intended!](#)

[Lecture 40 - How Local Rings Detect Smoothness or Nonsingularity in Algebraic Geometry](#)

[Lecture 41 - Any Variety is a Smooth Manifold with or without Non-Smooth Boundary](#)

[Lecture 42 - Any Variety is a Smooth Hypersurface On an Open Dense Subset](#)

Lecture 1 - Review of Ring Theory

Lecture 2 - Review of Ring Theory (Continued...)

Lecture 3 - Ideals in commutative rings

Lecture 4 - Operations on ideals

Lecture 5 - Properties of prime ideals

Lecture 6 - Colon and Radical of ideals

Lecture 7 - Radicals, extension and contraction of ideals

Lecture 8 - Modules and homomorphisms

Lecture 9 - Isomorphism theorems and Operations on modules

Lecture 10 - Operations on modules (Continued...)

Lecture 11 - Module homomorphism and determinant trick

Lecture 12 - Nakayama's lemma and exact sequences

Lecture 13 - Exact sequences (Continued...)

Lecture 14 - Homomorphisms and Tensor products

Lecture 15 - Properties of tensor products

Lecture 16 - Properties of tensor products (Continued...)

Lecture 17 - Tensor product of Algebras

Lecture 18 - Localization

Lecture 19 - Localization (Continued...)

Lecture 20 - Local properties

Lecture 21 - Further properties of localization

Lecture 22 - Integral dependence

Lecture 23 - Integral extensions

Lecture 24 - Lying over and Going-up theorems

Lecture 25 - Going-down theorem

Lecture 26 - Going-down theorem (Continued...)

Lecture 27 - Chain conditions

Lecture 28 - Noetherian and Artinian modules

Lecture 29 - Properties of Noetherian and Artinian modules, Composition Series

Lecture 30 - Further properties of Noetherian and Artinian modules and rings

Lecture 31 - Hilbert basis theorem and Primary decomposition

[Lecture 32 - Primary decomposition \(Continued...\)](#)

[Lecture 33 - Uniqueness of primary decomposition](#)

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[Lecture 38 - Hilberts Nullstellensatz](#)

- Lecture 1 - Introduction to Ordinary Differential Equations (ODE)
- Lecture 2 - Methods for First Order ODE's - Homogeneous Equations
- Lecture 3 - Methods for First order ODE's - Exact Equations
- Lecture 4 - Methods for First Order ODE's - Exact Equations (Continued...)
- Lecture 5 - Methods for First order ODE's - Reducible to Exact Equations
- Lecture 6 - Methods for First order ODE's - Reducible to Exact Equations (Continued...)
- Lecture 7 - Non-Exact Equations - Finding Integrating Factors
- Lecture 8 - Linear First Order ODE and Bernoulli's Equation
- Lecture 9 - Introduction to Second order ODE's
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Lecture 11 - Visualizing categorical and numerical data

Lecture 12 - Visualizing numerical data

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Lecture 16 - Sampling distribution of sample mean

Lecture 17 - Central Limit Theorem

Lecture 18 - Sampling distribution of sample variance and proportion

Lecture 19 - Python - Session 8

Lecture 20 - Python - Session 9

Lecture 21 - Sampling distribution of difference of sample means - Part 1

Lecture 22 - Sampling distribution of difference of sample means - Part 2

Lecture 23 - Sampling distribution of ratio of sample variances and difference of sample proportions

Lecture 24 - Python - Session 10

Lecture 25 - Python - Session 11

Lecture 26 - Point estimation - Part 1

Lecture 27 - Point estimation - Part 2

Lecture 28 - Point estimation - Part 3

Lecture 29 - Python - Session 12

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- Lecture 32 - EM algorithm - Part 1
- Lecture 33 - EM algorithm - Part 2
- Lecture 34 - Python - Session 14
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- Lecture 36 - Hypothesis Testing - Part 1
- Lecture 37 - Hypothesis Testing - Part 2
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- Lecture 39 - Python - Session 16
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- Lecture 41 - Hypothesis Testing for two sample problem - Part 1
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- Lecture 44 - Python - Session 18
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- Lecture 46 - Bootstrap Hypothesis Testing - Part 1
- Lecture 47 - Python - Session 20
- Lecture 48 - Python - Session 21
- Lecture 49 - Bootstrap Hypothesis Testing - Part 2
- Lecture 50 - Python - Session 22
- Lecture 51 - Confidence Interval Estimation - Part 1
- Lecture 52 - Confidence Interval Estimation - Part 2
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- Lecture 54 - Python - Session 23
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- Lecture 56 - Confidence interval for two sample problem
- Lecture 57 - Python - Session 25
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- Lecture 59 - Python - Session 26
- Lecture 60 - Python - Session 27

Lecture 1 - Introduction

Lecture 2 - Sample Space and Events

Lecture 3 - Special Events and Various Approaches to Defining Probability

Lecture 4 - Important Theorems

Lecture 5 - Numerical Examples and Introduction to Conditional Probability

Lecture 6 - Definition of Conditional Probability and Independence

Lecture 7 - Bayes' Theorem

Lecture 8 - Random Variable

Lecture 9 - Events Defined by a Random Variable

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Lecture 12 - Probability Mass Function

Lecture 13 - Continuous Random Variable and Probability Density Function

Lecture 14 - Numerical Examples

Lecture 15 - Moments

Lecture 16 - Higher Order Moments and Variance of a Random Variable

Lecture 17 - Numerical Examples of Moments and Bernoulli Distribution

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Lecture 23 - Application of Uniform Distribution and Exponential Distribution

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Lecture 28 - Numerical Examples of Normal Distributions

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Lecture 32 - Properties of the Joint Cumulative Distribution Function of a Bivariate Random Variable

Lecture 33 - Independence Between Two Random Variables

Lecture 34 - Examples of Joint Cumulative Distribution Functions, Marginals, and Independence

Lecture 35 - Joint Probability Mass Function, Marginal Probability Mass Function, Examples

Lecture 36 - Numerical Examples on Bivariate Discrete Random Variables and the Concept of Joint Probability

Lecture 37 - Marginal Probability Density Function, Independence, and Examples

Lecture 38 - Numerical Examples on Probability Density Function

Lecture 39 - Conditional Probability Mass Function

Lecture 40 - Conditional Probability Density Function

Lecture 41 - Moments for Bivariate Random Variables

Lecture 42 - Association Between Two Random Variables

Lecture 43 - Numerical Examples on Moments for Bivariate Random Variables

Lecture 44 - Conditional Mean and Variance for Discrete Random Variables

Lecture 45 - Conditional Mean and Variance for Continuous Random Variables

Lecture 46 - Numerical Examples on Conditional Mean and Variance

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Lecture 49 - Moments of a Multivariate Random Variable

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Lecture 57 - Convolution and Example on Transformation of n-variate Random Variables

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Lecture 60 - Example of Moment Generating Functions

Lecture 61 - Moment Generating Functions for the Transformation of Random Variables

Lecture 62 - Chebyshev's Inequality

Lecture 63 - Notions of Convergence, Law of Large Numbers, and the Central Limit Theorem

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Lecture 3 - The principle of inclusion and exclusion

Lecture 4 - Application of the principle of inclusion and exclusion

Lecture 5 - Fundamentals of logic

Lecture 6 - Logical Inferences

Lecture 7 - Methods of proof of an implication

Lecture 8 - First order logic (1)

Lecture 9 - First order logic (2)

Lecture 10 - Rules of inference for quantified propositions

Lecture 11 - Mathematical Induction (1)

Lecture 12 - Mathematical Induction (2)

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Lecture 14 - Probability, conditional probability

Lecture 15 - Independent events, Bayes theorem

Lecture 16 - Information and mutual information

Lecture 17 - Basic definition

Lecture 18 - Isomorphism and sub graphs

Lecture 19 - Walks, paths and circuits operations on graphs

Lecture 20 - Euler graphs, Hamiltonian circuits

Lecture 21 - Shortest path problem

Lecture 22 - Planar graphs

Lecture 23 - Basic definition

Lecture 24 - Properties of relations

Lecture 25 - Graph of relations

Lecture 26 - Matrix of relation

Lecture 27 - Closure of relation (1)

Lecture 28 - Closure of relation (2)

Lecture 29 - Warshall's algorithm

Lecture 30 - Partially ordered relation

Lecture 31 - Partially ordered sets

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[Lecture 34 - Boolean function \(1\)](#)

[Lecture 35 - Boolean function \(2\)](#)

[Lecture 36 - Discrete numeric function](#)

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[Lecture 38 - Introduction to recurrence relations](#)

[Lecture 39 - Second order recurrence relation with constant coefficients \(1\)](#)

[Lecture 40 - Second order recurrence relation with constant coefficients \(2\)](#)

[Lecture 41 - Application of recurrence relation](#)

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Lecture 2 - Linear dependence, independence and Wronskian of functions

Lecture 3 - Solution of second-order homogenous linear differential equations with constant coefficients - I

Lecture 4 - Solution of second-order homogenous linear differential equations with constant coefficients - II

Lecture 5 - Method of undetermined coefficients

Lecture 6 - Methods for finding Particular Integral for second-order linear differential equations with constant coefficients - I

Lecture 7 - Methods for finding Particular Integral for second-order linear differential equations with constant coefficients - II

Lecture 8 - Methods for finding Particular Integral for second-order linear differential equations with constant coefficients - III

Lecture 9 - Euler-Cauchy equations

Lecture 10 - Method of reduction for second-order linear differential equations

Lecture 11 - Method of variation of parameters

Lecture 12 - Solution of second order differential equations by changing dependent variable

Lecture 13 - Solution of second order differential equations by changing independent variable

Lecture 14 - Solution of higher-order homogenous linear differential equations with constant coefficients

Lecture 15 - Methods for finding Particular Integral for higher-order linear differential equations

Lecture 16 - Formulation of Partial differential equations

Lecture 17 - Solution of Lagrange's equation - I

Lecture 18 - Solution of Lagrange's equation - II

Lecture 19 - Solution of first order nonlinear equations - I

Lecture 20 - Solution of first order nonlinear equations - II

Lecture 21 - Solution of first order nonlinear equations - III

Lecture 22 - Solution of first order nonlinear equations - IV

Lecture 23 - Introduction to Laplace transforms

Lecture 24 - Laplace transforms of some standard functions

Lecture 25 - Existence theorem for Laplace transforms

Lecture 26 - Properties of Laplace transforms - I

Lecture 27 - Properties of Laplace transforms - II

Lecture 28 - Properties of Laplace transforms - III

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Lecture 30 - Convolution theorem for Laplace transforms - I

Lecture 31 - Convolution theorem for Laplace transforms - II

- Lecture 32 - Initial and final value theorems for Laplace transforms
- Lecture 33 - Laplace transforms of periodic functions
- Lecture 34 - Laplace transforms of Heaviside unit step function
- Lecture 35 - Laplace transforms of Dirac delta function
- Lecture 36 - Applications of Laplace transforms - I
- Lecture 37 - Applications of Laplace transforms - II
- Lecture 38 - Applications of Laplace transforms - III
- Lecture 39 - Z-transform and inverse Z-transform of elementary functions
- Lecture 40 - Properties of Z-transforms - I
- Lecture 41 - Properties of Z-transforms - II
- Lecture 42 - Initial and final value theorem for Z-transforms
- Lecture 43 - Convolution theorem for Z-transforms
- Lecture 44 - Applications of Z-transforms - I
- Lecture 45 - Applications of Z-transforms - II
- Lecture 46 - Applications of Z-transforms - III
- Lecture 47 - Fourier series and its convergence - I
- Lecture 48 - Fourier series and its convergence - II
- Lecture 49 - Fourier series of even and odd functions
- Lecture 50 - Fourier half-range series
- Lecture 51 - Parseval's Identity
- Lecture 52 - Complex form of Fourier series
- Lecture 53 - Fourier integrals
- Lecture 54 - Fourier sine and cosine integrals
- Lecture 55 - Fourier transforms
- Lecture 56 - Fourier sine and cosine transforms
- Lecture 57 - Convolution theorem for Fourier transforms
- Lecture 58 - Applications of Fourier transforms to BVP - I
- Lecture 59 - Applications of Fourier transforms to BVP - II
- Lecture 60 - Applications of Fourier transforms to BVP - III

Lecture 1 - Definition and classification of linear integral equations

Lecture 2 - Conversion of IVP into integral equations

Lecture 3 - Conversion of BVP into an integral equations

Lecture 4 - Conversion of integral equations into differential equations

Lecture 5 - Integro-differential equations

Lecture 6 - Fredholm integral equation with separable kernel: Theory

Lecture 7 - Fredholm integral equation with separable kernel: Examples

Lecture 8 - Solution of integral equations by successive substitutions

Lecture 9 - Solution of integral equations by successive approximations

Lecture 10 - Solution of integral equations by successive approximations: Resolvent kernel

Lecture 11 - Fredholm integral equations with symmetric kernels: Properties of eigenvalues and eigenfunctions

Lecture 12 - Fredholm integral equations with symmetric kernels: Hilbert Schmidt theory

Lecture 13 - Fredholm integral equations with symmetric kernels: Examples

Lecture 14 - Construction of Green function - I

Lecture 15 - Construction of Green function - II

Lecture 16 - Green function for self adjoint linear differential equations

Lecture 17 - Green function for non-homogeneous boundary value problem

Lecture 18 - Fredholm alternative theorem - I

Lecture 19 - Fredholm alternative theorem - II

Lecture 20 - Fredholm method of solutions

Lecture 21 - Classical Fredholm theory: Fredholm first theorem - I

Lecture 22 - Classical Fredholm theory: Fredholm first theorem - II

Lecture 23 - Classical Fredholm theory: Fredholm second theorem and third theorem

Lecture 24 - Method of successive approximations

Lecture 25 - Neumann series and resolvent kernels - I

Lecture 26 - Neumann series and resolvent kernels - II

Lecture 27 - Equations with convolution type kernels - I

Lecture 28 - Equations with convolution type kernels - II

Lecture 29 - Singular integral equations - I

Lecture 30 - Singular integral equations - II

Lecture 31 - Cauchy type integral equations - I

- Lecture 32 - Cauchy type integral equations - II
- Lecture 33 - Cauchy type integral equations - III
- Lecture 34 - Cauchy type integral equations - IV
- Lecture 35 - Cauchy type integral equations - V
- Lecture 36 - Solution of integral equations using Fourier transform
- Lecture 37 - Solution of integral equations using Hilbert transform - I
- Lecture 38 - Solution of integral equations using Hilbert transform - II
- Lecture 39 - Calculus of variations: Introduction
- Lecture 40 - Calculus of variations: Basic concepts - I
- Lecture 41 - Calculus of variations: Basic concepts - II
- Lecture 42 - Calculus of variations: Basic concepts and Euler equation
- Lecture 43 - Euler equation: Some particular cases
- Lecture 44 - Euler equation : A particular case and Geodesics
- Lecture 45 - Brachistochrone problem and Euler equation - I
- Lecture 46 - Euler's equation - II
- Lecture 47 - Functions of several independent variables
- Lecture 48 - Variational problems in parametric form
- Lecture 49 - Variational problems of general type
- Lecture 50 - Variational derivative and invariance of Euler's equation
- Lecture 51 - Invariance of Euler's equation and isoperimetric problem - I
- Lecture 52 - Isoperimetric problem - II
- Lecture 53 - Variational problem involving a conditional extremum - I
- Lecture 54 - Variational problem involving a conditional extremum - II
- Lecture 55 - Variational problems with moving boundaries - I
- Lecture 56 - Variational problems with moving boundaries - II
- Lecture 57 - Variational problems with moving boundaries - III
- Lecture 58 - Variational problems with moving boundaries; One sided variation
- Lecture 59 - Variational problem with a movable boundary for a functional dependent on two functions
- Lecture 60 - Hamilton's principle: Variational principle of least action

NPTEL : NOC:Nonlinear Programming (Mathematics)

Co-ordinators : S. K. Gupta

Lecture 1 - Convex Sets and Functions

Lecture 2 - Properties of Convex Functions - I

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Lecture 4 - Properties of Convex Functions- III

Lecture 5 - Convex Programming Problems

Lecture 6 - KKT optimality conditions

Lecture 7 - Quadratic Programming Problems - I

Lecture 8 - Quadratic Programming Problems - II

Lecture 9 - Separable Programming - I

Lecture 10 - Separable Programming - II

Lecture 11 - Geometric Programming - I

Lecture 12 - Geometric Programming - II

Lecture 13 - Geometric Programming - III

Lecture 14 - Dynamic Programming - I

Lecture 15 - Dynamic Programming - II

Lecture 16 - Dynamic programming approach to find shortest path in any network

Lecture 17 - Dynamic Programming - IV

Lecture 18 - Search Techniques - I

Lecture 19 - Search Techniques - II

Lecture 20 - Search Techniques - III

Lecture 1 - Introduction to error analysis and linear systems

Lecture 2 - Gaussian elimination with Partial pivoting

Lecture 3 - LU decomposition

Lecture 4 - Jacobi and Gauss Seidel methods

Lecture 5 - Iterative methods-II

Lecture 6 - Introduction to Non-linear equations and Bisection method

Lecture 7 - Regula Falsi and Secant methods

Lecture 8 - Newton-Raphson method

Lecture 9 - Fixed point iteration method

Lecture 10 - System of Nonlinear equations

Lecture 11 - Introduction to Eigenvalues and Eigenvectors

Lecture 12 - Similarity Transformations and Gershgorin Theorem

Lecture 13 - Jacobi's Method for Computing Eigenvalues

Lecture 14 - Power Method

Lecture 15 - Inverse Power Method

Lecture 16 - Interpolation - Part I (Introduction to Interpolation)

Lecture 17 - Interpolation - Part II (Some basic operators and their properties)

Lecture 18 - Interpolation - Part III (Newton's Forward/ Backward difference and derivation of general error)

Lecture 19 - Interpolation - Part IV (Error in approximating a function by a polynomial using Newton's Forward and Backward difference formula)

Lecture 20 - Interpolation - Part V (Solving problems using Newton's Forward and Backward difference formula)

Lecture 21 - Interpolation - Part VI (Central difference formula)

Lecture 22 - Interpolation - Part VII (Lagrange interpolation formula with examples)

Lecture 23 - Interpolation - Part VIII (Divided difference interpolation with examples)

Lecture 24 - Interpolation - Part IX (Hermite's interpolation with examples)

Lecture 25 - Numerical differentiation - Part I (Introduction to numerical differentiation by interpolation formula)

Lecture 26 - Numerical differentiation - Part II (Numerical differentiation based on Lagrange's interpolation with examples)

Lecture 27 - Numerical differentiation - Part III (Numerical differentiation based on Divided difference formula with examples)

Lecture 28 - Numerical differentiation - Part IV (Maxima and minima of a tabulated function and differentiation errors)

Lecture 29 - Numerical differentiation - Part V (Differentiation based on finite difference operators)

Lecture 30 - Numerical differentiation - Part VI (Method of undetermined coefficients and Derivatives with unequal intervals)

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[Lecture 31 - Numerical Integration - Part I \(Methodology of Numerical Integration and Rectangular rule \)](#)

[Lecture 32 - Numerical Integration - Part II \(Quadrature formula and Trapezoidal rule with associated errors\)merical Integration Part-I \(Methodology of Numerical Integration and Rectangular rule \)](#)

[Lecture 33 - Numerical Integration - Part III \(Simpsons 1/3rd rule with associated errors\)](#)

[Lecture 34 - Numerical Integration - Part IV \(Composite Simpsons 1/3rd rule and Simpsons 3/8th rule with examples\)](#)

[Lecture 35 - Numerical Integration - Part V \(Gauss Legendre 2-point and 3-point formula with examples\)](#)

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[Lecture 37 - Numerical methods for ODE-1](#)

[Lecture 38 - Numerical Methods - II](#)

[Lecture 39 - R-K Methods for solving ODEs](#)

[Lecture 40 - Multi-step Method for solving ODEs](#)

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Lecture 2 - Determinant of a Matrix

Lecture 3 - Rank of a Matrix

Lecture 4 - Vector Space - I

Lecture 5 - Vector Space - II

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Lecture 7 - Bases and Dimension - I

Lecture 8 - Bases and Dimension - II

Lecture 9 - Linear Transformation - I

Lecture 10 - Linear Transformation - II

Lecture 11 - Orthogonal Subspaces

Lecture 12 - Row Space, Column Space and Null Space

Lecture 13 - Eigen Values and Eigen Vectors - I

Lecture 14 - Eigen Values and Eigen Vectors - II

Lecture 15 - Diagonalizable Matrices

Lecture 16 - Orthogonal Sets

Lecture 17 - Gram Schmidt orthogonalization and orthogonal bases

Lecture 18 - Introduction to Matlab

Lecture 19 - Sign Integer Representation

Lecture 20 - Computer Representation of Numbers

Lecture 21 - Floating Point Representation

Lecture 22 - Round-off Error

Lecture 23 - Error Propagation in Computer Arithmetic

Lecture 24 - Addition and Multiplication of Floating Point Numbers

Lecture 25 - Conditioning and Condition Numbers - I

Lecture 26 - Conditioning and Condition Numbers - II

Lecture 27 - Stability of Numerical Algorithms - I

Lecture 28 - Stability of Numerical Algorithms - II

Lecture 29 - Vector Norms - I

Lecture 30 - Vector Norms - II

Lecture 31 - Matrix Norms - I

- Lecture 32 - Matrix Norms - II
- Lecture 33 - Convergent Matrices - I
- Lecture 34 - Convergent Matrices - II
- Lecture 35 - Stability of non linear system
- Lecture 36 - Condition number of a matrix: Elementary Properties
- Lecture 37 - Sensitivity Analysis - I
- Lecture 38 - Sensitivity Analysis - II
- Lecture 39 - Residual Theorem
- Lecture 40 - Nearness to Singularity
- Lecture 41 - Estimation of the Condition Number
- Lecture 42 - Singular value decomposition of a matrix - I
- Lecture 43 - Singular value decomposition of a matrix - II
- Lecture 44 - Orthonormal Projections
- Lecture 45 - Algebraic and geometric properties of SVD
- Lecture 46 - SVD and their applications
- Lecture 47 - Perturbation theorem for singular values
- Lecture 48 - Outer product expansion of a matrix
- Lecture 49 - Least square solutions - I
- Lecture 50 - Least square solutions - II
- Lecture 51 - Householder matrices
- Lecture 52 - Householder matrices and their applications
- Lecture 53 - Householder QR factorization - I
- Lecture 54 - Householder QR factorization - II
- Lecture 55 - Basic theorems on eigenvalues and QR method
- Lecture 56 - Power Method
- Lecture 57 - Rate of Convergence of Power Method
- Lecture 58 - Applications of Power Method with Shift
- Lecture 59 - Jacobi Method - I
- Lecture 60 - Jacobi Method - II

Lecture 1 - Introduction to Numerical solutions

Lecture 2 - Numerical Solution of ODE

Lecture 3 - Numerical solution of PDE

Lecture 4 - Finite difference approximation

Lecture 5 - Polynomial fitting and one-sided approximation

Lecture 6 - Solution of parabolic equation

Lecture 7 - Implicit and C-N scheme for solving 1D parabolic equation

Lecture 8 - Stability analysis of Explicit scheme for solving parabolic equation

Lecture 9 - Stability of Crank-Nicoloson's scheme

Lecture 10 - Approximation of derivative boundary conditions

Lecture 11 - Solution of two-dimensional parabolic equation

Lecture 12 - Solution of 2D parabolic equation using ADI scheme

Lecture 13 - Solution of Elliptic Equation

Lecture 14 - Solution of Elliptic equation using SOR method

Lecture 15 - Solution of Elliptic equation using ADI scheme

Lecture 16 - Solution of Hyperbolic equation

Lecture 17 - Stability analysis for Hyperbolic equations

Lecture 18 - Characteristics of PDE

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Lecture 20 - Wendroff's method

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- Lecture 2 - Limits for multivariable functions - I
- Lecture 3 - Limits for multivariable functions - II
- Lecture 4 - Continuity of multivariable functions
- Lecture 5 - Partial Derivatives - I
- Lecture 6 - Partial Derivatives - II
- Lecture 7 - Differentiability - I
- Lecture 8 - Differentiability - II
- Lecture 9 - Chain rule - I
- Lecture 10 - Chain rule - II
- Lecture 11 - Change of variables
- Lecture 12 - Euler's theorem for homogeneous functions
- Lecture 13 - Tangent planes and Normal lines
- Lecture 14 - Extreme values - I
- Lecture 15 - Extreme values - II
- Lecture 16 - Lagrange multipliers
- Lecture 17 - Taylor's theorem
- Lecture 18 - Error approximation
- Lecture 19 - Polar-curves
- Lecture 20 - Multiple Integrals
- Lecture 21 - Change Of Order Of Integration
- Lecture 22 - Change of Variables in Multiple Integral
- Lecture 23 - Introduction to Gamma Function
- Lecture 24 - Introduction to Beta Function
- Lecture 25 - Properties of Beta and Gamma Functions - I
- Lecture 26 - Properties of Beta and Gamma Functions - II
- Lecture 27 - Dirichlet's Integral
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- Lecture 29 - Vector Differentiation
- Lecture 30 - Gradient of a Scalar Field and Directional Derivative
- Lecture 31 - Normal Vector and Potential field

[Lecture 32 - Gradient \(Identities\), Divergence and Curl \(Identities\)](#)

[Lecture 33 - Some Identities on Divergence and Curl](#)

[Lecture 34 - Line Integral \(I\)](#)

[Lecture 35 - Applications of Line Integrals](#)

[Lecture 36 - Green's Theorem](#)

[Lecture 37 - Surface Area](#)

[Lecture 38 - Surface Integral](#)

[Lecture 39 - Divergence Theorem of Gauss](#)

[Lecture 40 - Stoke's Theorem](#)

Lecture 1 - Introduction to differential equations - I

Lecture 2 - Introduction to differential equations - II

Lecture 3 - Existence and uniqueness of solutions of differential equations - I

Lecture 4 - Existence and uniqueness of solutions of differential equations - II

Lecture 5 - Existence and uniqueness of solutions of differential equations - III

Lecture 6 - Existence and uniqueness of solutions of a system of differential equations

Lecture 7 - Linear System

Lecture 8 - Properties of Homogeneous Systems

Lecture 9 - Solution of Homogeneous Linear System with Constant Coefficients - I

Lecture 10 - Solution of Homogeneous Linear System with Constant Coefficients - II

Lecture 11 - Solution of Homogeneous Linear System with Constant Coefficients - III

Lecture 12 - Solution of Non-Homogeneous Linear System with Constant Coefficients

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Lecture 14 - Uniform Convergence of Power Series

Lecture 15 - Power Series Solution of Second Order Homogeneous Equations

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Lecture 18 - Regular singular points - III

Lecture 19 - Regular singular points - IV

Lecture 20 - Regular singular points - V

Lecture 21 - Critical points

Lecture 22 - Stability of Linear Systems - I

Lecture 23 - Stability of Linear Systems - II

Lecture 24 - Stability of Linear Systems - III

Lecture 25 - Critical Points and Paths of Non-linear Systems

Lecture 26 - Boundary value problems for second order differential equations

Lecture 27 - Self - adjoint Forms

Lecture 28 - Sturm - Liouville problem and its properties

Lecture 29 - Sturm - Liouville problem and its applications

Lecture 30 - Green's function and its applications - I

Lecture 31 - Green's function and its applications - II

- Lecture 32 - Origins and Classification of First Order PDE
- Lecture 33 - Initial Value Problem for Quasi-linear First Order Equations
- Lecture 34 - Existence and Uniqueness of Solutions
- Lecture 35 - Surfaces orthogonal to a given system of surfaces
- Lecture 36 - Nonlinear PDE of first order
- Lecture 37 - Cauchy method of characteristics - I
- Lecture 38 - Cauchy method of characteristics - II
- Lecture 39 - Compatible systems of first order equations
- Lecture 40 - Charpit's method - I
- Lecture 41 - Charpit's method - II
- Lecture 42 - Second Order PDE with Variable Coefficients
- Lecture 43 - Classification and Canonical Form of Second Order PDE - I
- Lecture 44 - Classification and Canonical Form of Second Order PDE - II
- Lecture 45 - Classification and Characteristic Curves of Second Order PDEs
- Lecture 46 - Review of Integral Transforms - I
- Lecture 47 - Review of Integral Transforms - II
- Lecture 48 - Review of Integral Transforms - II
- Lecture 49 - Review of Integral Transforms - III
- Lecture 50 - Laplace Equation - I
- Lecture 51 - Laplace Equation - II
- Lecture 52 - Laplace and Poisson Equations
- Lecture 53 - One dimensional wave equation and its solution - I
- Lecture 54 - One dimensional wave equation and its solution - II
- Lecture 55 - One dimensional wave equation and its solution - III
- Lecture 56 - Two dimensional wave equation and its solution - I
- Lecture 57 - Solution of non-homogeneous wave equation
- Lecture 58 - Solution of homogeneous diffusion equation - I
- Lecture 59 - Solution of homogeneous diffusion equation - II
- Lecture 60 - Duhamel's principle

- Lecture 1 - Elementary row operations
- Lecture 2 - Echelon form of a matrix
- Lecture 3 - Rank of a matrix
- Lecture 4 - System of Linear Equations - I
- Lecture 5 - System of Linear Equations - II
- Lecture 6 - Introduction to Vector Spaces
- Lecture 7 - Subspaces
- Lecture 8 - Basis and Dimension
- Lecture 9 - Linear Transformations
- Lecture 10 - Rank and Nullity
- Lecture 11 - Inverse of a Linear Transformation
- Lecture 12 - Matrix Associated with a LT
- Lecture 13 - Eigenvalues and Eigenvectors
- Lecture 14 - Cayley-Hamilton Theorem and Minimal Polynomial
- Lecture 15 - Diagonalization
- Lecture 16 - Special Matrices
- Lecture 17 - More on Special Matrices and Gerschgorin Theorem
- Lecture 18 - Inner Product Spaces
- Lecture 19 - Vector and Matrix Norms
- Lecture 20 - Gram Schmidt Process
- Lecture 21 - Normal Matrices
- Lecture 22 - Positive Definite Matrices
- Lecture 23 - Positive Definite and Quadratic Forms
- Lecture 24 - Gram Matrix and Minimization of Quadratic Forms
- Lecture 25 - Generalized Eigenvectors and Jordan Canonical Form
- Lecture 26 - Evaluation of Matrix Functions
- Lecture 27 - Least Square Approximation
- Lecture 28 - Singular Value Decomposition
- Lecture 29 - Pseudo-Inverse and SVD
- Lecture 30 - Introduction to Ill-Conditioned Systems
- Lecture 31 - Regularization of Ill-Conditioned Systems

[Lecture 32 - Linear Systems: Iterative Methods - I](#)

[Lecture 33 - Linear Systems: Iterative Methods - II](#)

[Lecture 34 - Non-Stationary Iterative Methods: Steepest Descent - I](#)

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[Lecture 36 - Krylov Subspace Iterative Methods \(Conjugate Gradient Method\)](#)

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[Lecture 38 - Introduction to Positive Matrices](#)

[Lecture 39 - Positive Matrices, Positive Eigenpair, Perron Root and vector, Example](#)

[Lecture 40 - Polar Decomposition](#)

Lecture 1 - Introduction to Mathematical Modeling

Lecture 2 - Discrete Time Linear Models in Population Dynamics - I

Lecture 3 - Discrete Time Linear Models in Population Dynamics - II

Lecture 4 - Discrete Time Linear Age Structured Models

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Lecture 7 - Analysis on Logistic Difference Equation

Lecture 8 - Classifications of Bifurcation

Lecture 9 - Discrete Time Non - Linear Models in Population Dynamics - II

Lecture 10 - Discrete Time Prey - Predator Model

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Lecture 13 - Continuous Time Models in Population Dynamics - I

Lecture 14 - Continuous Time Models in Population Dynamics - II

Lecture 15 - Stability and Linearization of System of Ordinary Differential Equations

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- Lecture 6 - Representation of Lie algebras
- Lecture 7 - Classification of 2 dimensional representation of two dimensional non-abelian Lie algebra
- Lecture 8 - Isomorphism Theorem
- Lecture 9 - Characterization of completely reducible module
- Lecture 10 - Representation theory of $sl_2(\mathbb{C})$
- Lecture 11 - Irreducible representation of $sl_2(\mathbb{C})$
- Lecture 12 - Irreducible representation of $sl_2(\mathbb{C})$ (Continued...)
- Lecture 13 - Complete reducibility of $sl_2(\mathbb{C})$
- Lecture 14 - Complete reducibility of $sl_2(\mathbb{C})$ (Continued...)
- Lecture 15 - Representation theory of $sl_2(\mathbb{C})$ -basic observation
- Lecture 16 - Application of $sl_2(\mathbb{C})$ representation theory in combinatorics
- Lecture 17 - Constructions of new representations
- Lecture 18 - Construction of universal algebras - I
- Lecture 19 - Construction of universal algebras - II
- Lecture 20 - Non-degenerate and invariant bilinear forms
- Lecture 21 - Schur's lemma and Killing form
- Lecture 22 - Killing form of general and special linear Lie algebras
- Lecture 23 - The universal enveloping algebra
- Lecture 24 - Properties of the universal enveloping algebra
- Lecture 25 - The Casimir operator for representations of $gl_n(\mathbb{C})$ and $sl_n(\mathbb{C})$
- Lecture 26 - Weyl's theorem of complete reducibility
- Lecture 27 - The structure of $sl_{n+1}(\mathbb{C})$
- Lecture 28 - Representations of $sl_{n+1}(\mathbb{C})$ - I
- Lecture 29 - Representations of $sl_{n+1}(\mathbb{C})$ - II
- Lecture 30 - Representations of $sl_{n+1}(\mathbb{C})$ - III
- Lecture 31 - Casimir operator and highest weight modules - I

- Lecture 32 - Casimir operator and highest weight modules - II
- Lecture 33 - Irreducible representations of $sl_{n+1}(C)$
- Lecture 34 - Verma module and its irreducible quotient
- Lecture 35 - Verma modules and standard cyclic irreducible modules
- Lecture 36 - Finite dimensional standard cyclic irreducible modules
- Lecture 37 - Standard cyclic irreducible modules
- Lecture 38 - Character Theory - I
- Lecture 39 - Character Theory - II
- Lecture 40 - Denominator Identity - Prep 1
- Lecture 41 - Denominator Identity - Prep 2
- Lecture 42 - Proof of the denominator identity
- Lecture 43 - Freudenthal's formula
- Lecture 44 - The Weyl character formula
- Lecture 45 - The Laplacian operator and the Weyl Character Formula
- Lecture 46 - Proof of the Weyl Character Formula
- Lecture 47 - Applications of Weyl Character formula
- Lecture 48 - The Weyl dimension formula, Schur polynomials
- Lecture 49 - Semi-standard Young Tableaux
- Lecture 50 - BGG resolution